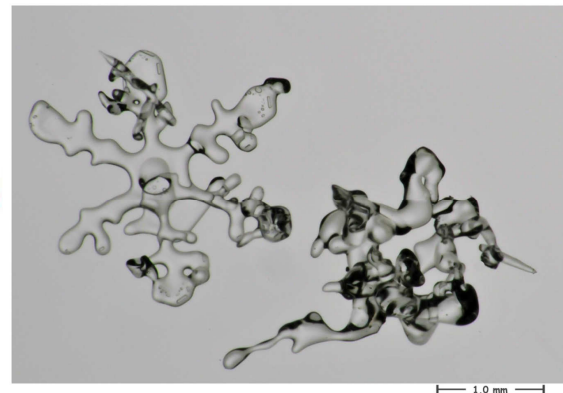
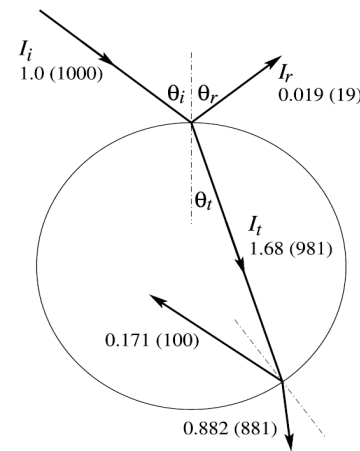
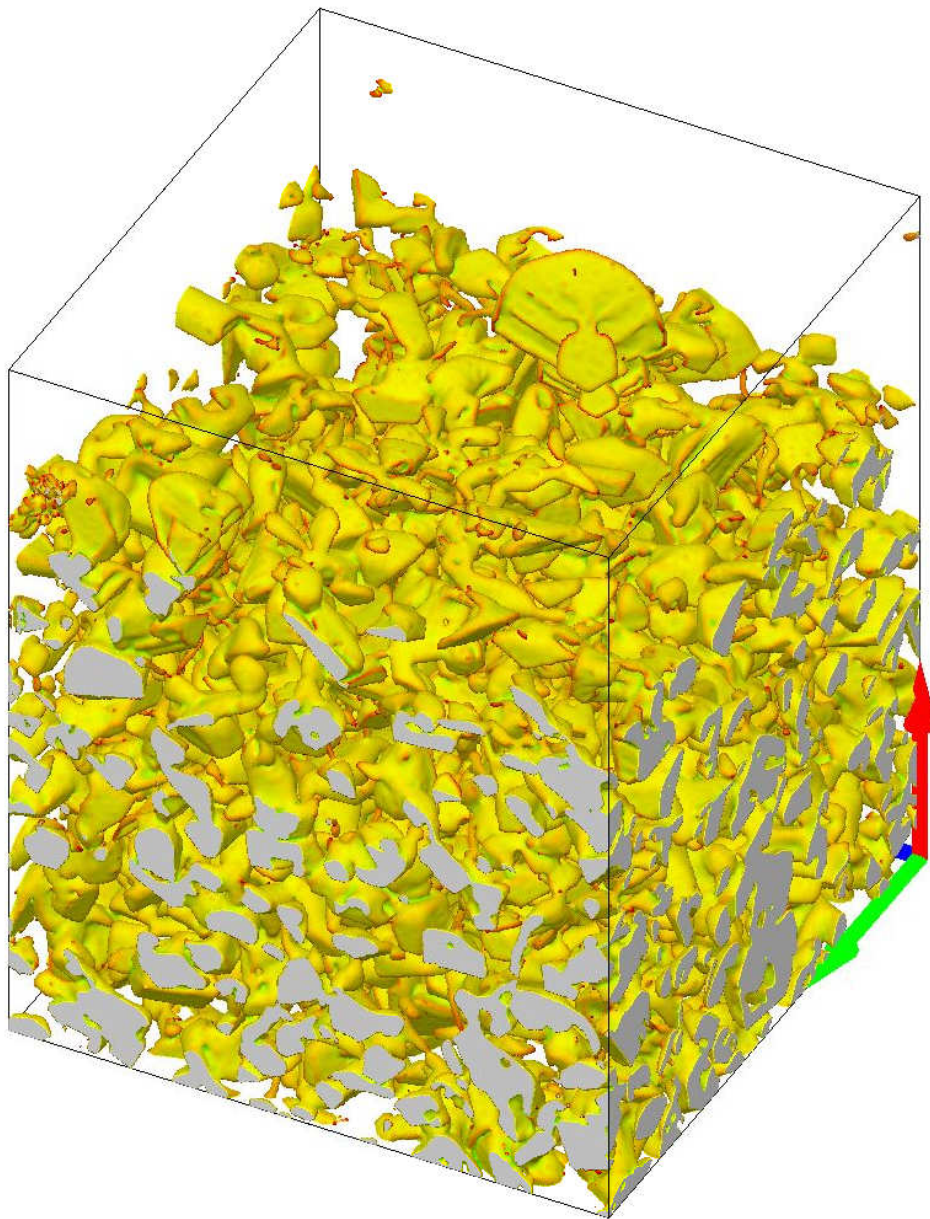


# Study of the reflectance of snow based on measurements and modeling

8/7/2015, Frédéric Flin



**Alexander Regenscheit M2R 2014**

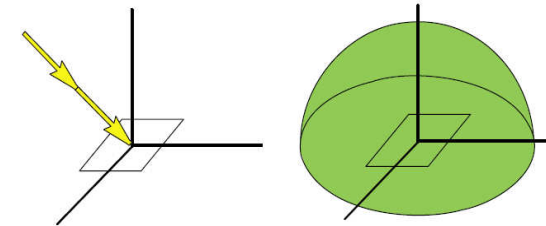
Supervised by  
Marie Dumont and Frédéric Flin

# Definitions

## ➤ Albedo:

- Ratio between reflected radiation into the **whole hemisphere** over the incident irradiance

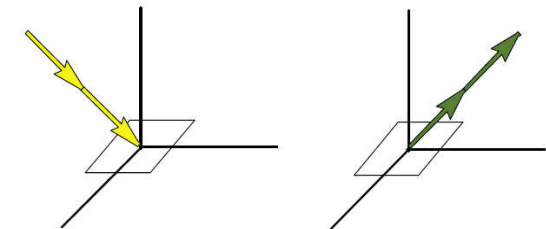
Directional-hemispherical



## ➤ Bidirectional reflection density function (BRDF):

- Ratio of reflected radiance in an **infinitesimal solid angle direction** over the incident irradiance of a collimated beam

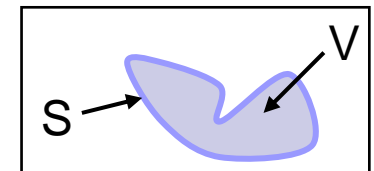
Bidirectional



## ➤ Specific Surface Area (SSA):

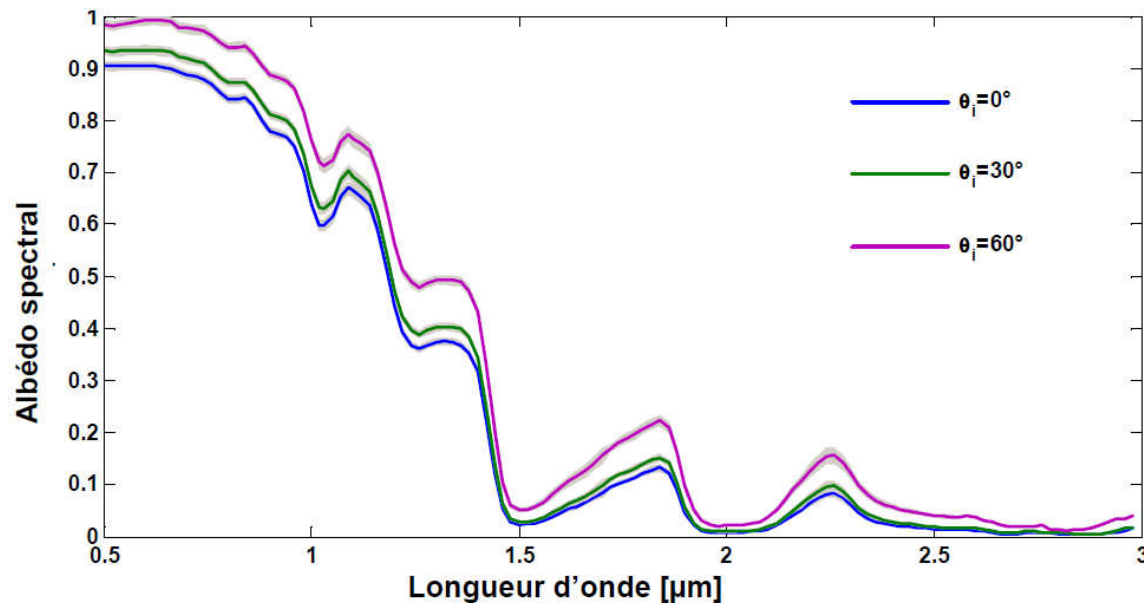
- Ratio between surface (interface ice/air) and volume of ice
- Measure for grain size

$$SSA = \frac{S}{V \cdot \rho_{glace}}$$

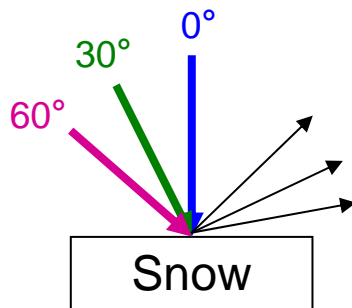
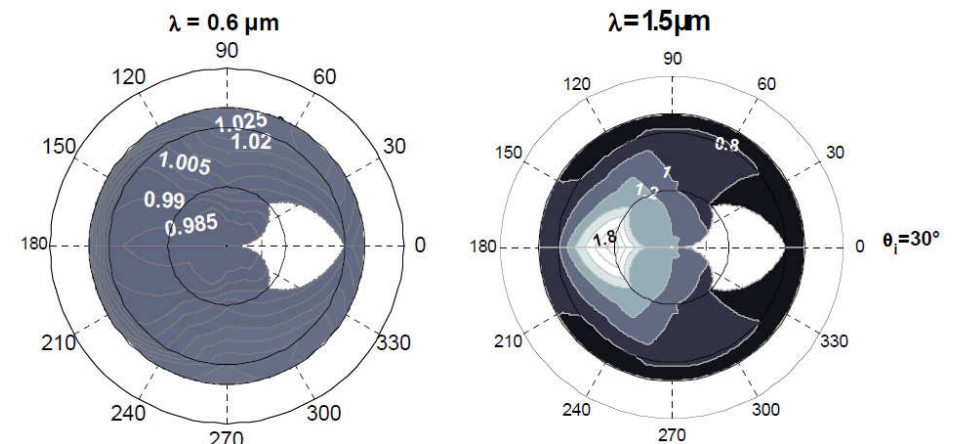


# Optical properties of snow

## Albedo

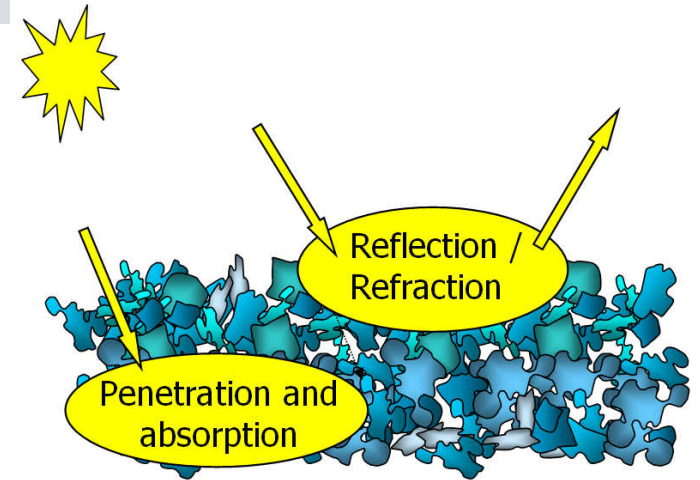


## BRDF

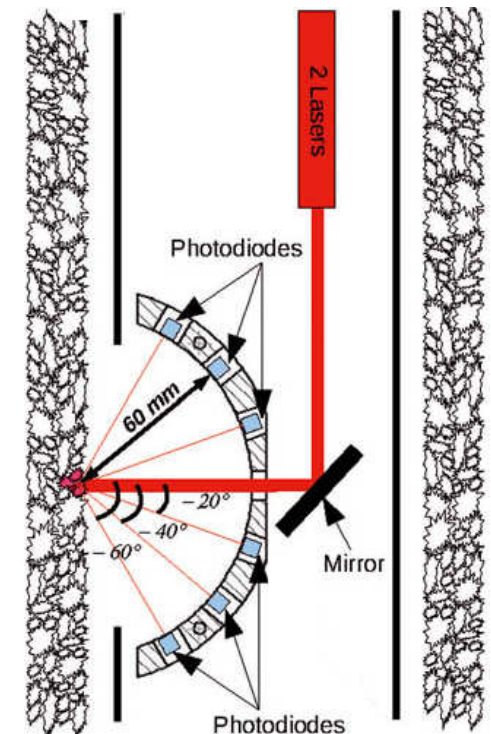


- dominant multiscattering  $\lambda < 1 \mu\text{m}$
- strong forward scattering for  $\lambda > 1 \mu\text{m}$  (absorption)

# Motivation



- Application of optical properties of snow :
  - Modeling of the snowpack (energy balance) (Brun et al., 1989)
  - Remote sensing of reflectance (Dumont, 2010)
  - In situ measurements of SSA (DUFISSS, POSSSUM) (Arnaud, 2011)
- Albedo and BRDF depending on the microstructure of snow (Haussener et al. 2012; Picard et al., 2009; Kaempfer et al., 2007)







# Motivation

For a better understanding of the relation between microstructure and optical properties:

- BRDF measurements of two different snow types were done 2012/13 (IPAG) together with taking tomography images of this snow (3SR)

## Goal of the internship

- Comparison of these measurements with the results of different models
- Comparison of different models with each other
- Evaluating the range of correctness of the models
- Impact of grain shape on BRDF



# Content

- Measurements
- Models
- Results
- Conclusion

# Measurements

Sampling for BRDF measurements at IPAG



Sampling for tomography at 3SR Lab



- +Grain photographs
- +Density measurements
- +SSA measurements

Before and after BRDF  
measurements

# Measurements

Sampling for BRDF measurements at IPAG



Sampling for tomography at 3SR Lab



Fig. 1. Overview of the BRDF measurement setup

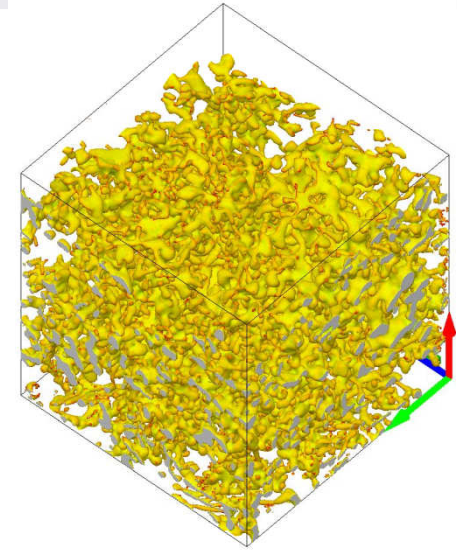


# Measurements

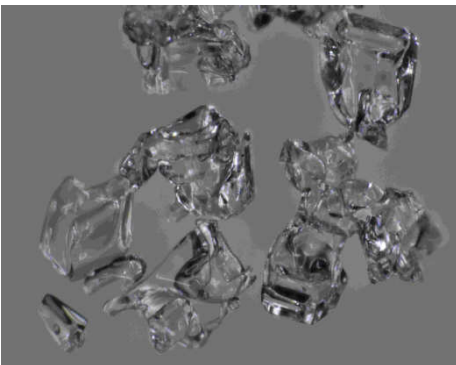
## ➤ March 2012 – recent snow



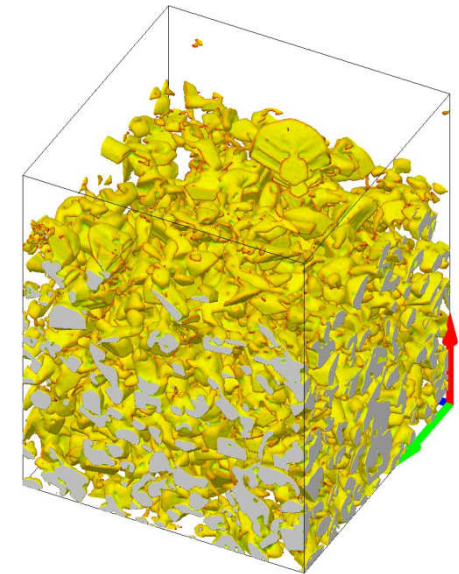
- Naturally deposited snow
- Three tomography images (3SRLab)
- 5 reflectance measurement configurations (IPAG)



## ➤ March 2013 – faceted snow



- 17 days under temperature gradient
- Sieved snow
- Two tomography images
- 9 reflectance measurement configurations



# Models:

Microstructural properties → optical properties

- **DISORT**: (Stamnes, 1988)
  - Exact solution of the radiative transfer equation
  - Mie-scattering (spheres)
- **Photon tracking model PBRT**: (Malgat, 2012)
  - Optical law based probability model
  - Calculates reflectance from digital images
- **Analytical model**: (Kokhanovsky, 2012)
  - Approximation of the radiative transfer equation,
  - Based on reflection function for snow grains,
  - Valid for weakly absorbing media
  - Two free parameters:
    - $M$  as a measure for the impurities
    - $L = b^2d$  ( $b$  = shape factor;  $d$  = mean diameter of grains)

→ To compare measurements with the models the SSA has to be equivalent



# Results

## ➤ Albedo:

- DISORT vs PBRT for image of spheres
- DISORT vs PBRT for tomography images of snow
- DISORT and PBRT vs measurements

## ➤ BRDF:

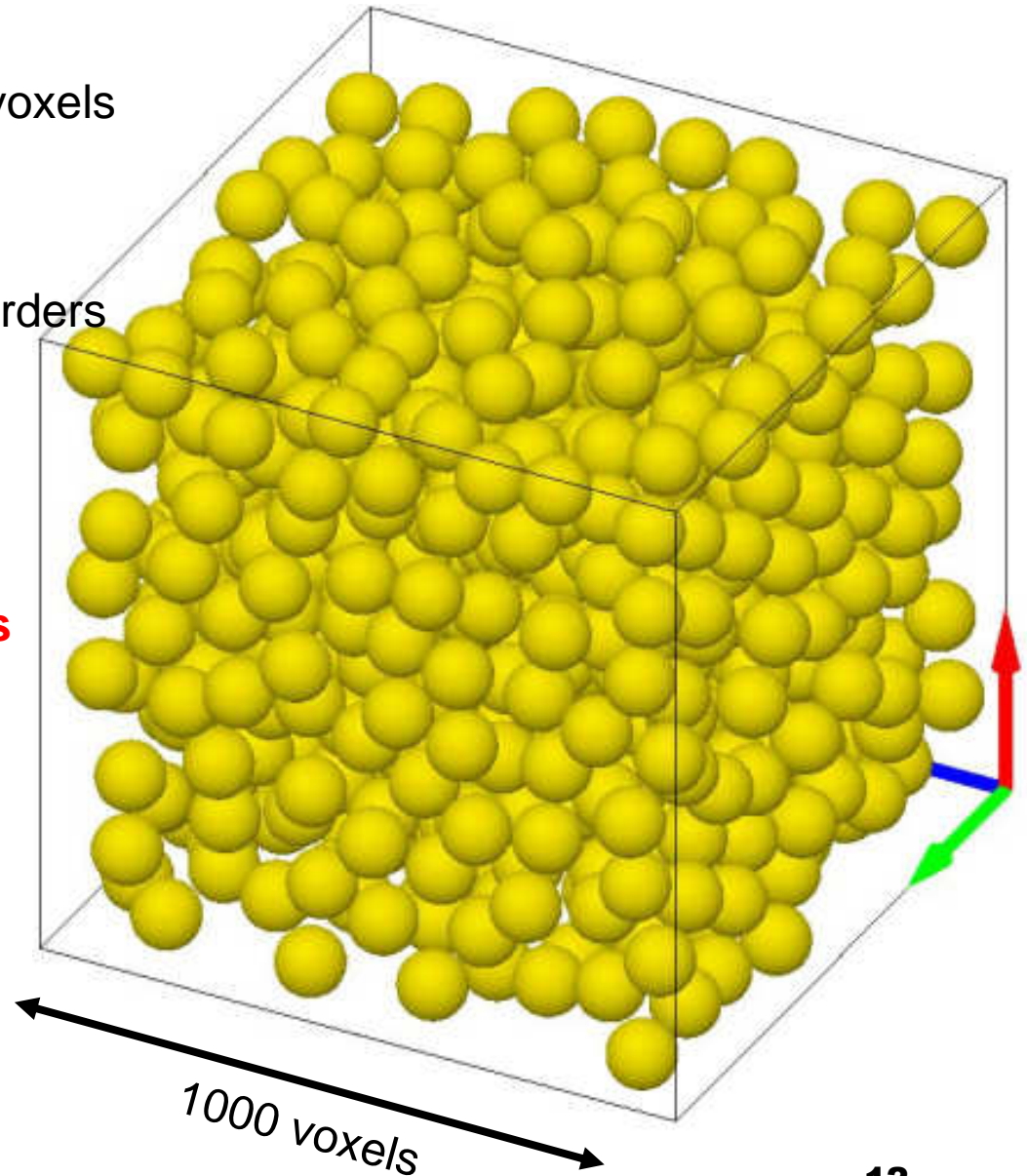
- Measurements vs analytical model
- Measurements of different snow grains

# Albedo – DISORT vs PBRT - spheres

## Numerical samples:

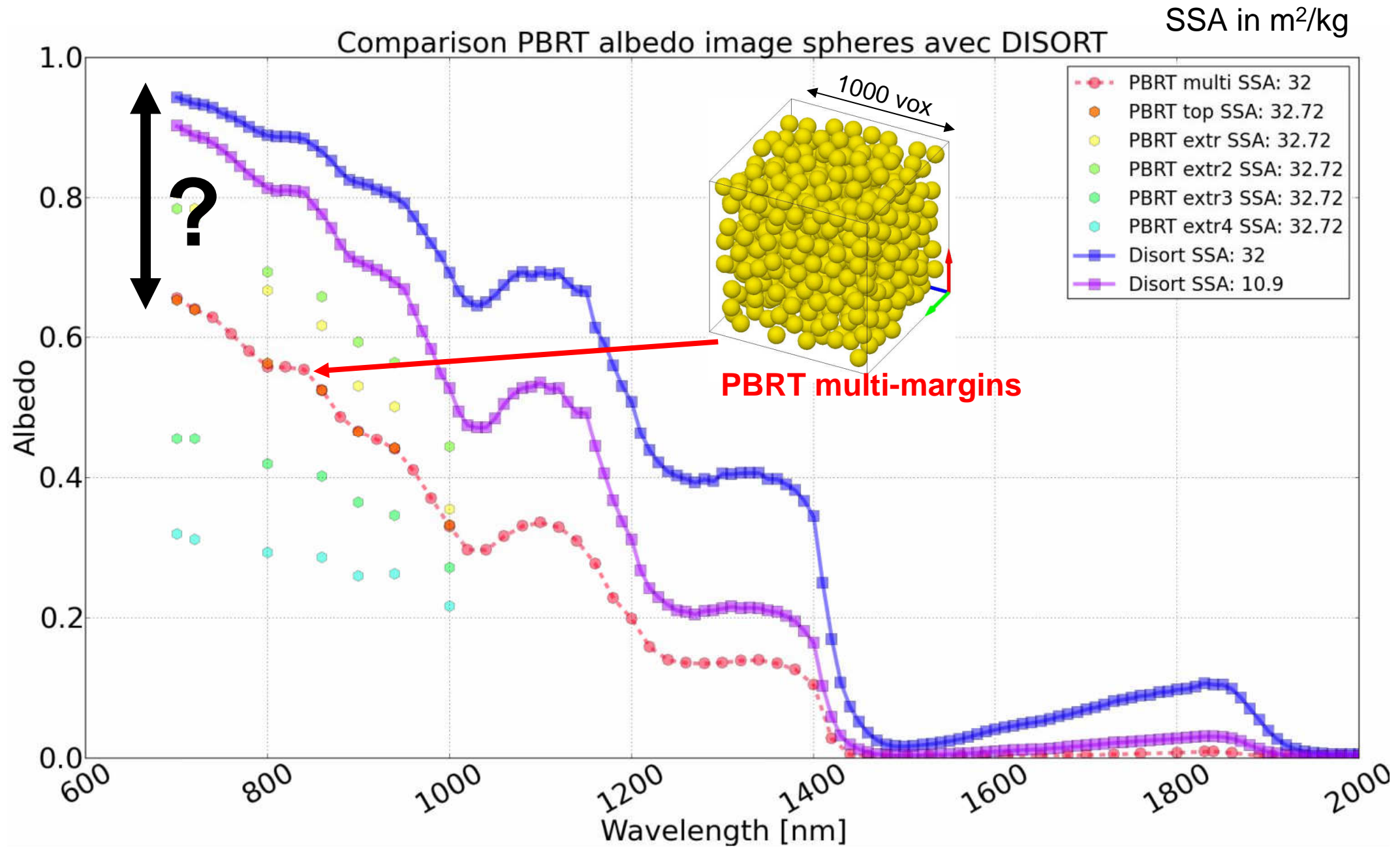
- 600 non-overlapping spheres of  $r = 50$  voxels
- Scaling on  $r$ 
  - density =  $288 \text{ kg/m}^3$
  - SSA =  $32.72 \text{ m}^2/\text{kg}$
- spheres do not intersect the image borders

**PBRT multi-margins**

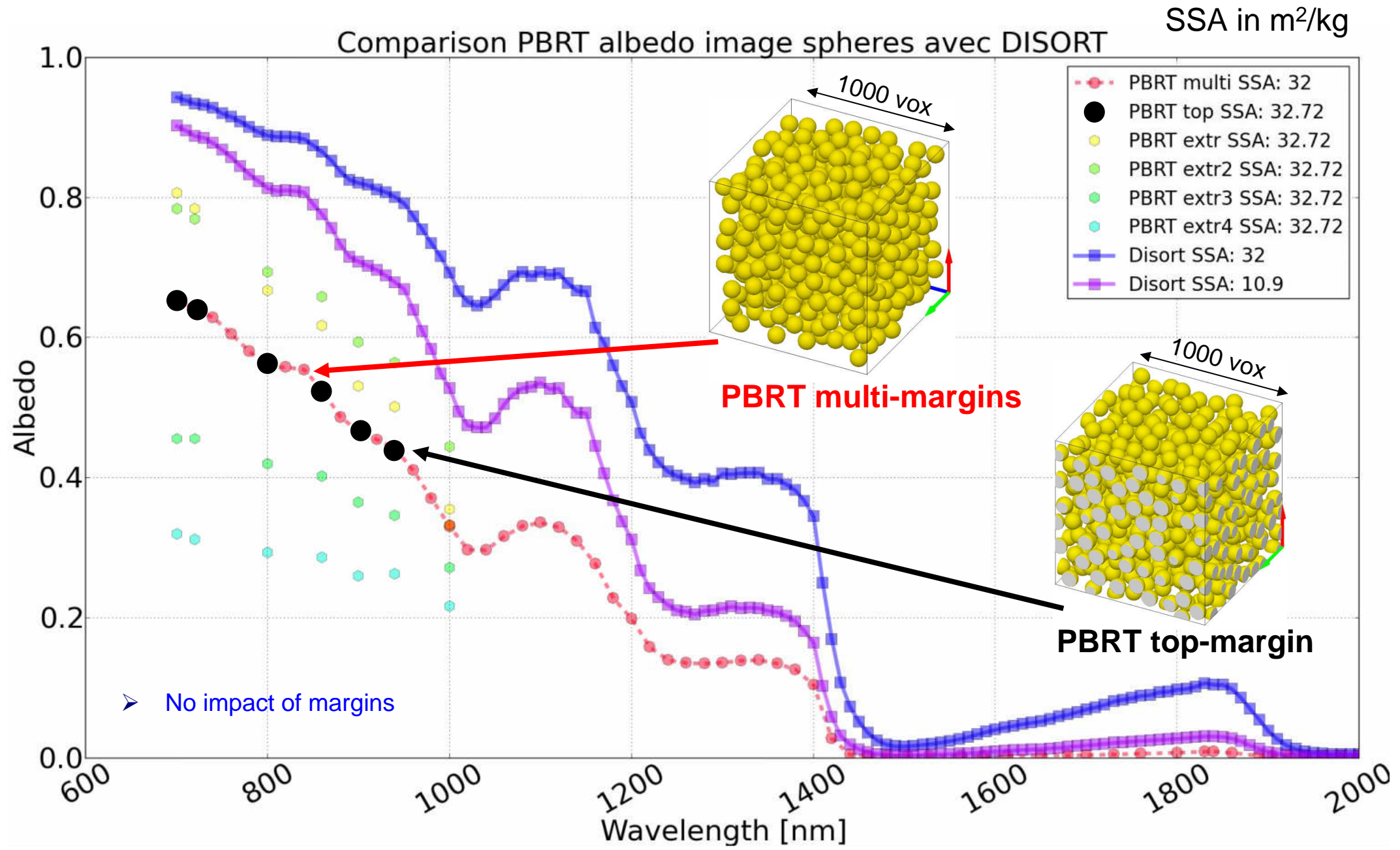




# Albedo – DISORT vs PBRT - spheres

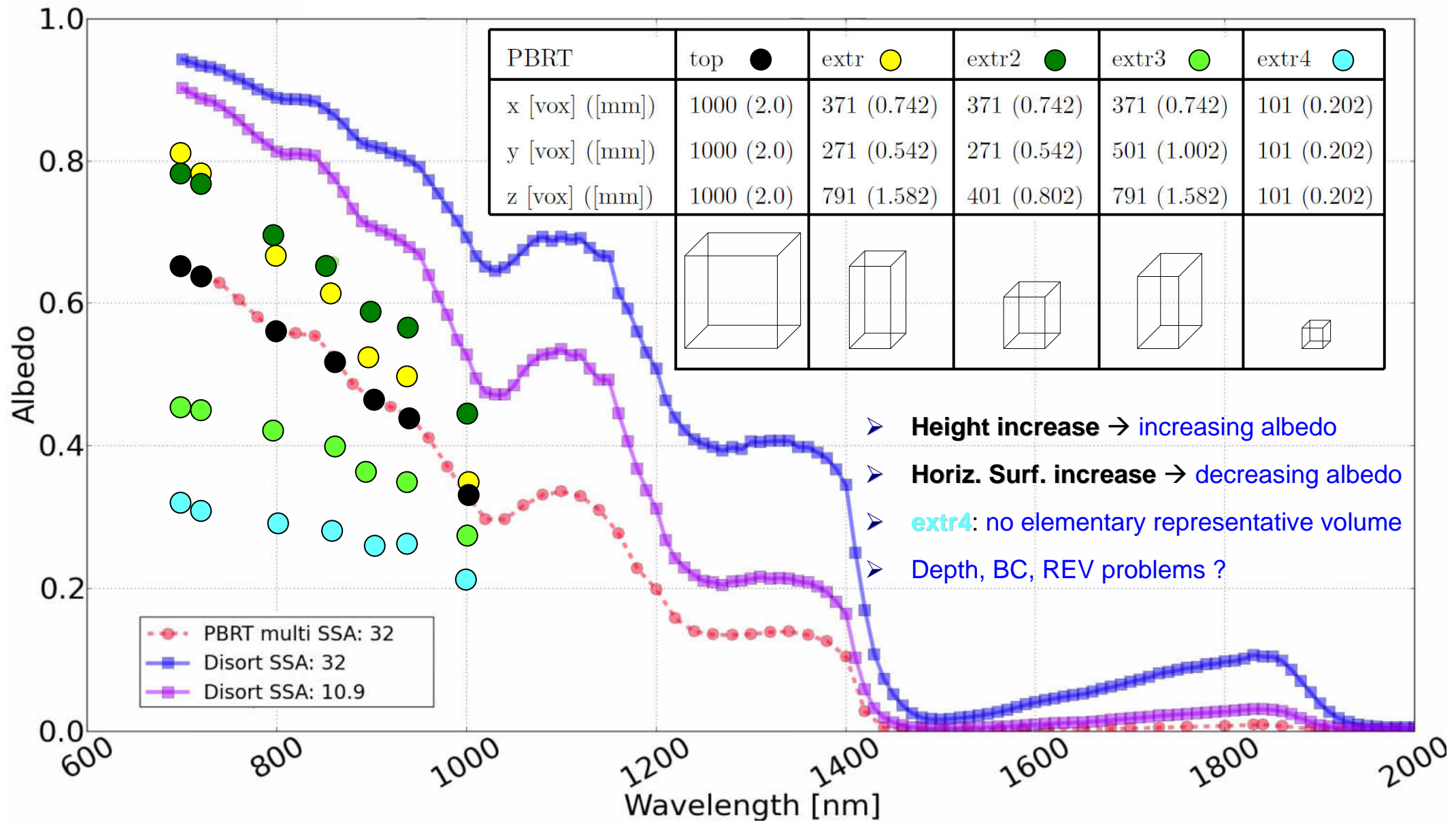


# Albedo – DISORT vs PBRT - spheres



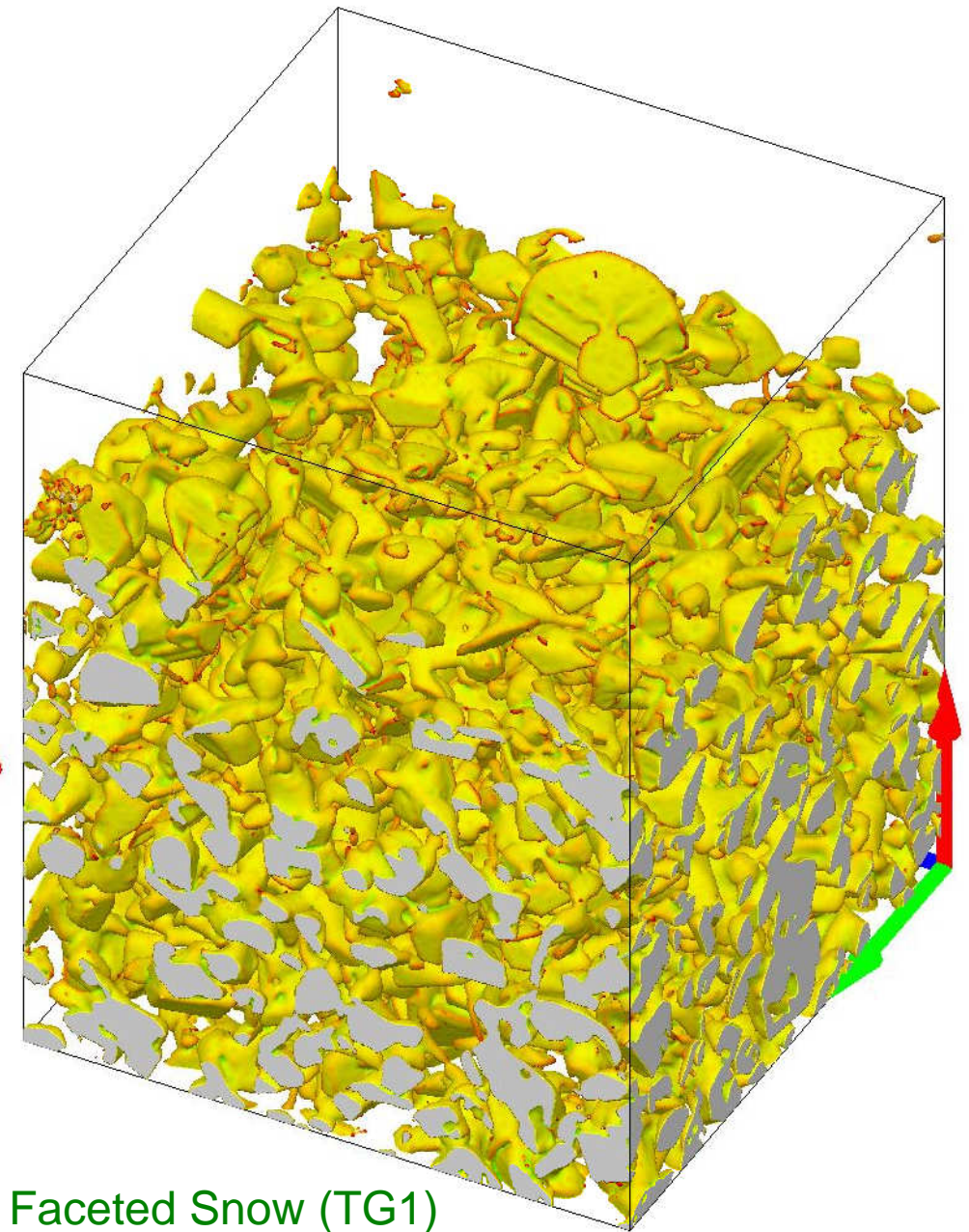
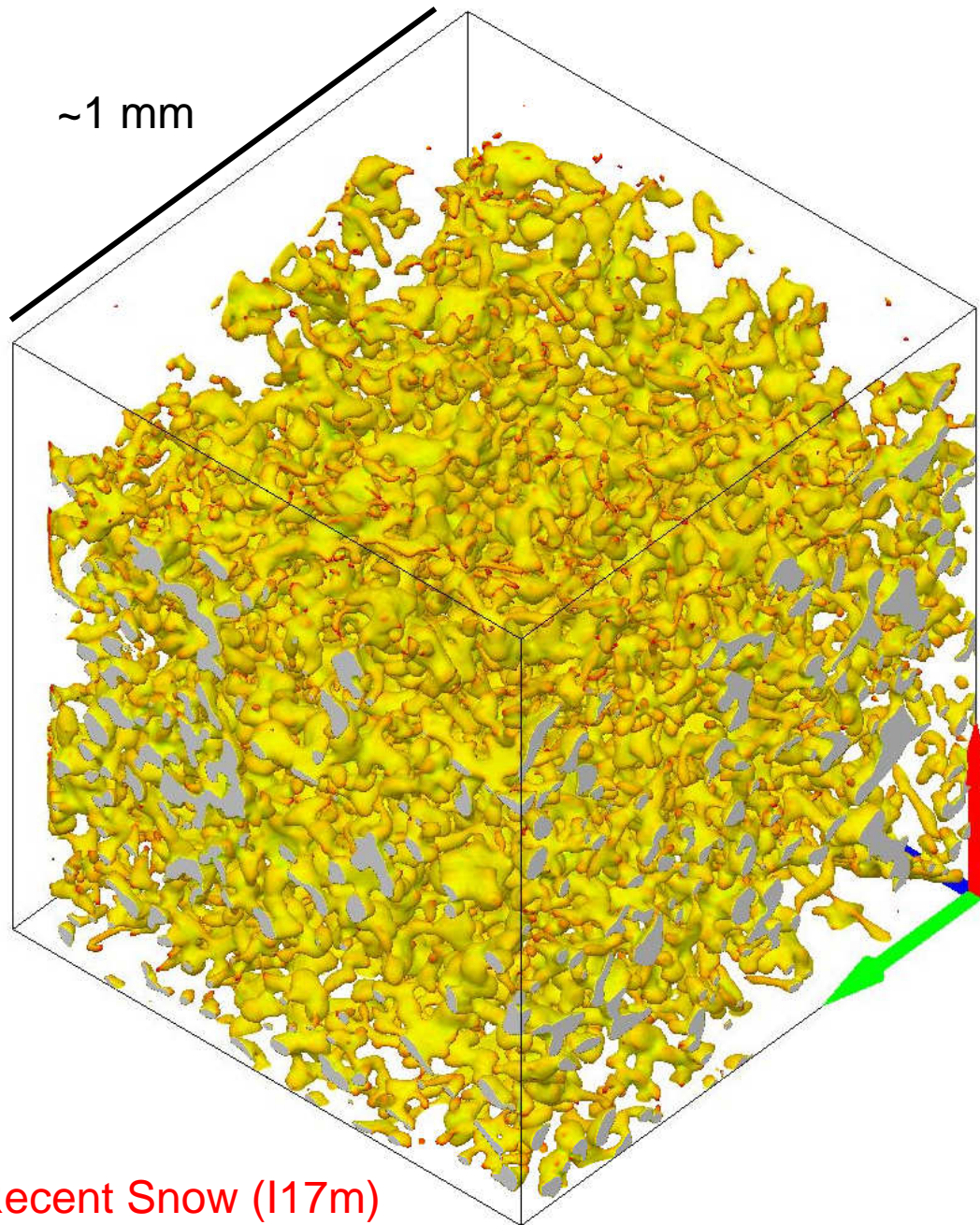
# Albedo – DISORT vs PBRT - spheres

SSA in  $\text{m}^2/\text{kg}$



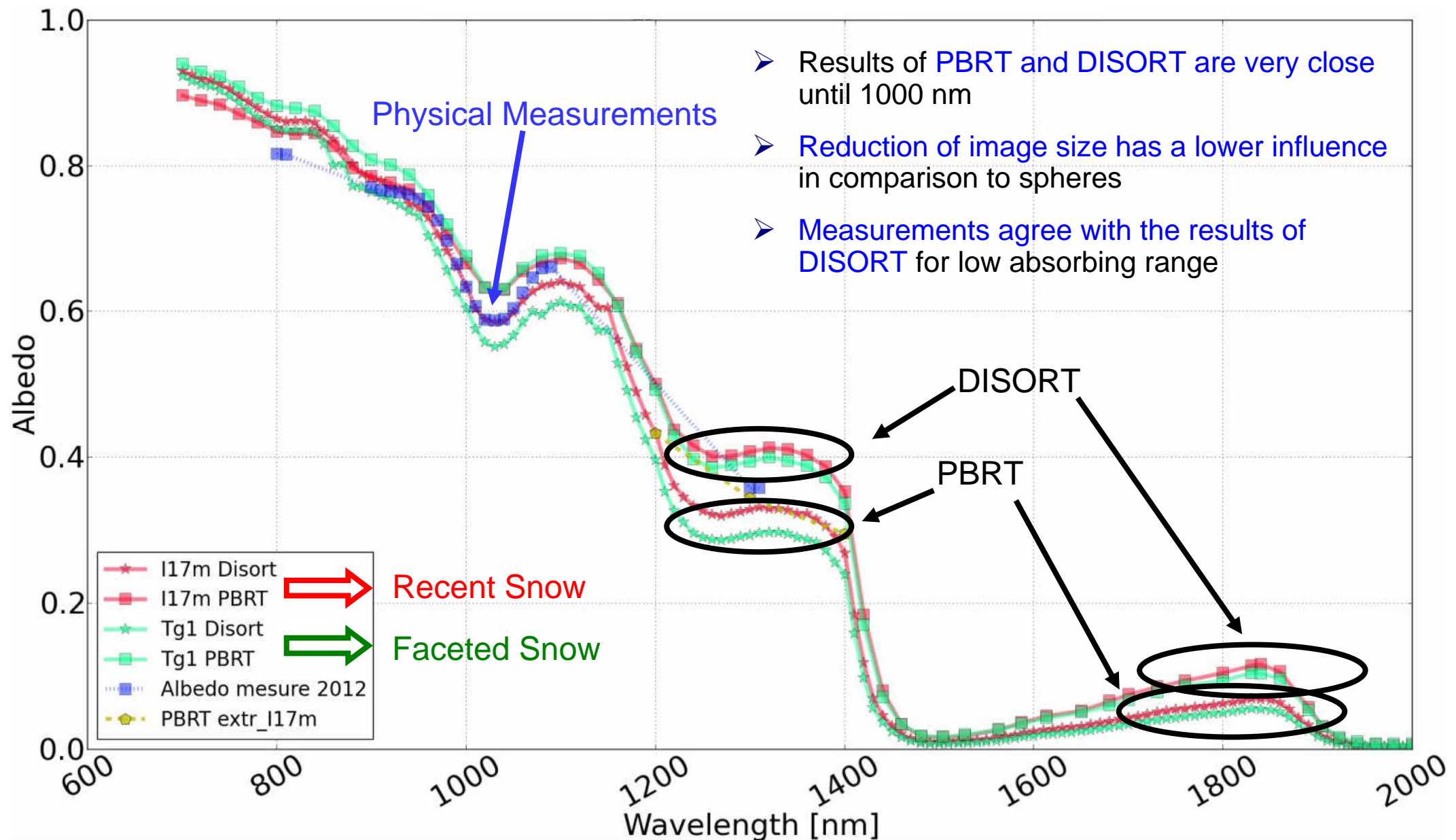


# Albedo – DISORT vs PBRT - snow





# Albedo – DISORT vs PBRT - snow





# Albedo – DISORT vs PBRT

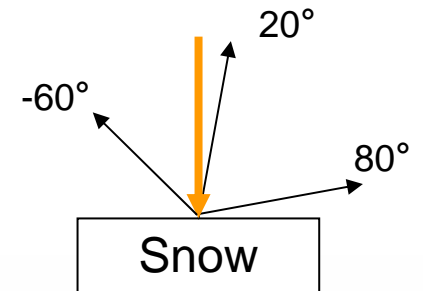
- Results depending strongly on image size
- Tomography images deliver PBRT results closer to DISORT than spheres
- Size effect is stronger for the spheres than for the tomography images
- Measurements confirm DISORT in weak absorbing range

# BRDF – Analytical Model vs Measurements

- Influence of impurities (M) was neglected ( $\lambda \geq 800$  nm)
- $L = b^2d$  :
  - $d = 6 / (SSA \cdot \rho)$
  - $b = 3.6$  shape factor for spheres

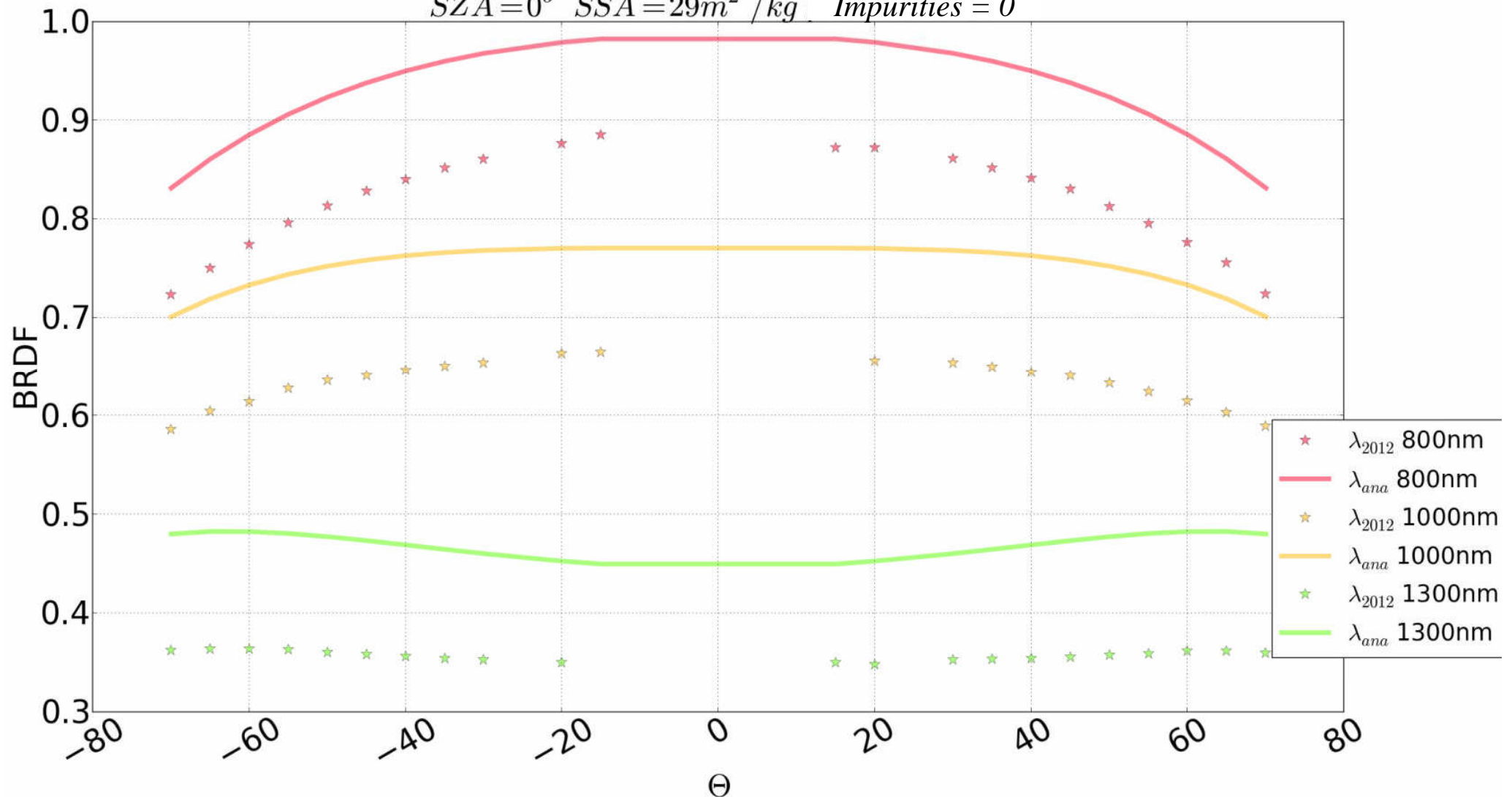


# BRDF – Analytical Model vs Measurements



Comparaison mesures 2012 et modele analytique

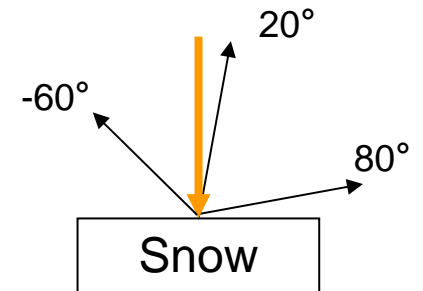
$SZA = 0^\circ$   $SSA = 29m^2/kg$   $Impurities = 0$





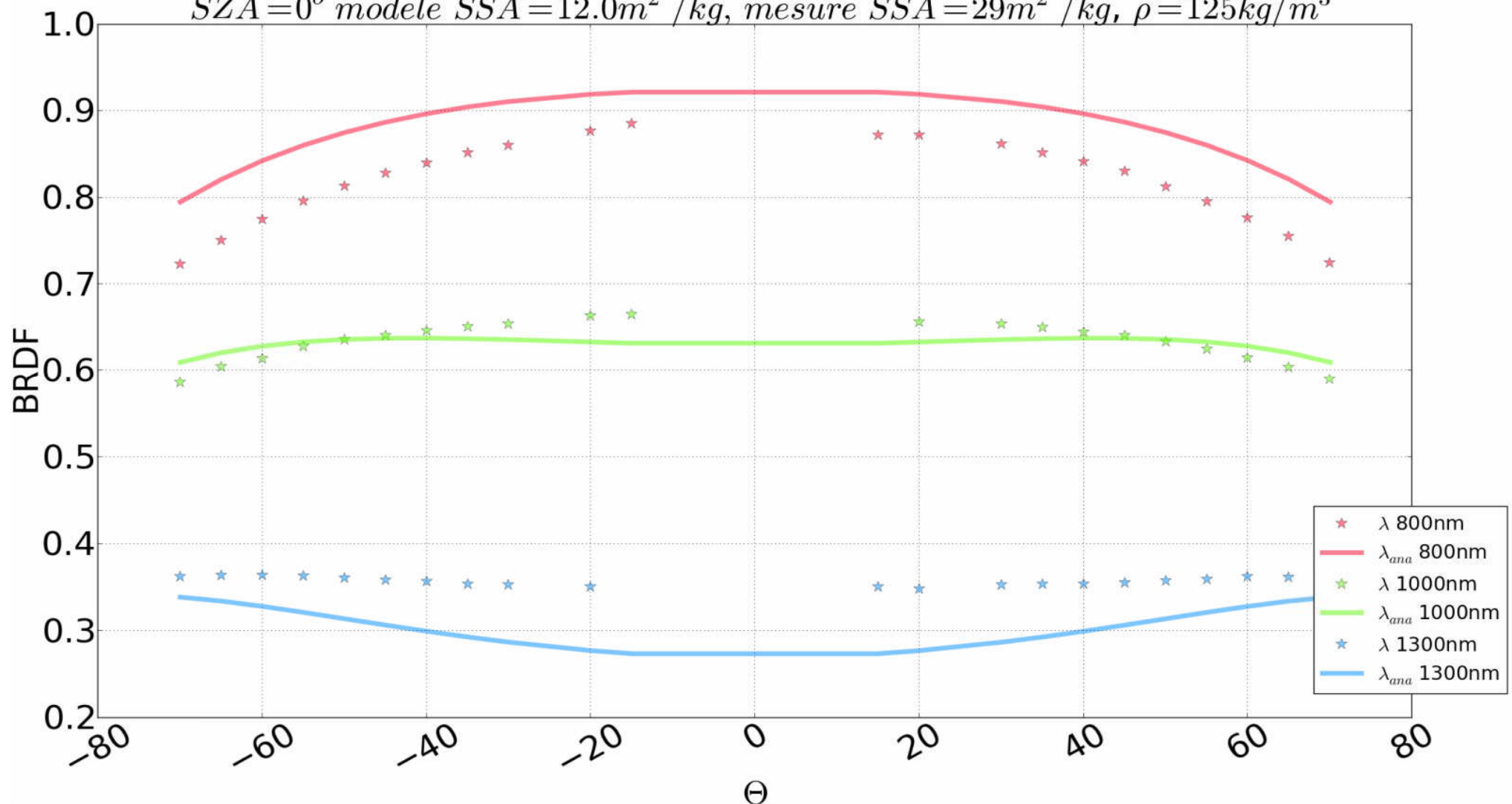
# BRDF – Analytical Model vs Measurements

Adjusted using SSA



Comparaison mesures 2012 et modele analytique

$SZA = 0^\circ$  modele  $SSA = 12.0 m^2 / kg$ , mesure  $SSA = 29 m^2 / kg$ ,  $\rho = 125 kg / m^3$



# BRDF – Analytical Model vs Measurements

- Influence of impurities (M) was neglected ( $\lambda \geq 800$  nm)
- $L = b^2d$  :
  - $d = 6 / (SSA \cdot \rho)$
  - $b = 3.6$  shape factor for spheres
  - $b = 5.6$  shape factor for non-spherical grains





# BRDF – Analytical Model vs Measurements

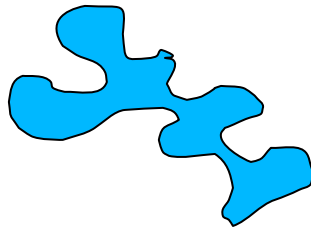
- Strong deviation between model and measurements for spherical shape
- Adaption of the model by varying the shape factor reduces the deviation between model and measurements
- Shape factor for non-spherical grains is in agreement with the real grain shape for recent snow
- Model is more isotropic for 800 nm and 1000 nm, however less isotropic for 1300 nm than the measurements

# BRDF – Impact of grain shape

- To investigate the impact of the grain shape the measurements of two different types of snow are compared:

- Recent snow 2012

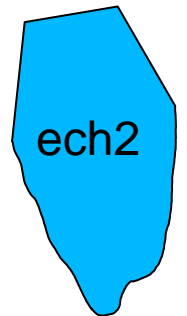
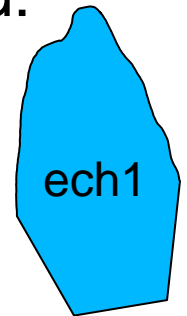
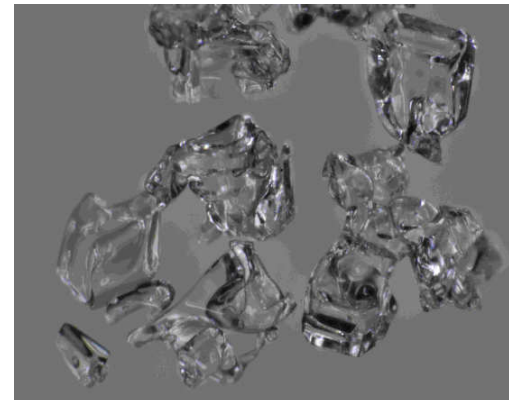
→ rounded shape



- Faceted snow 2013

→ rounded shape on the top (ech1)

→ faceted shape on the top (ech2)

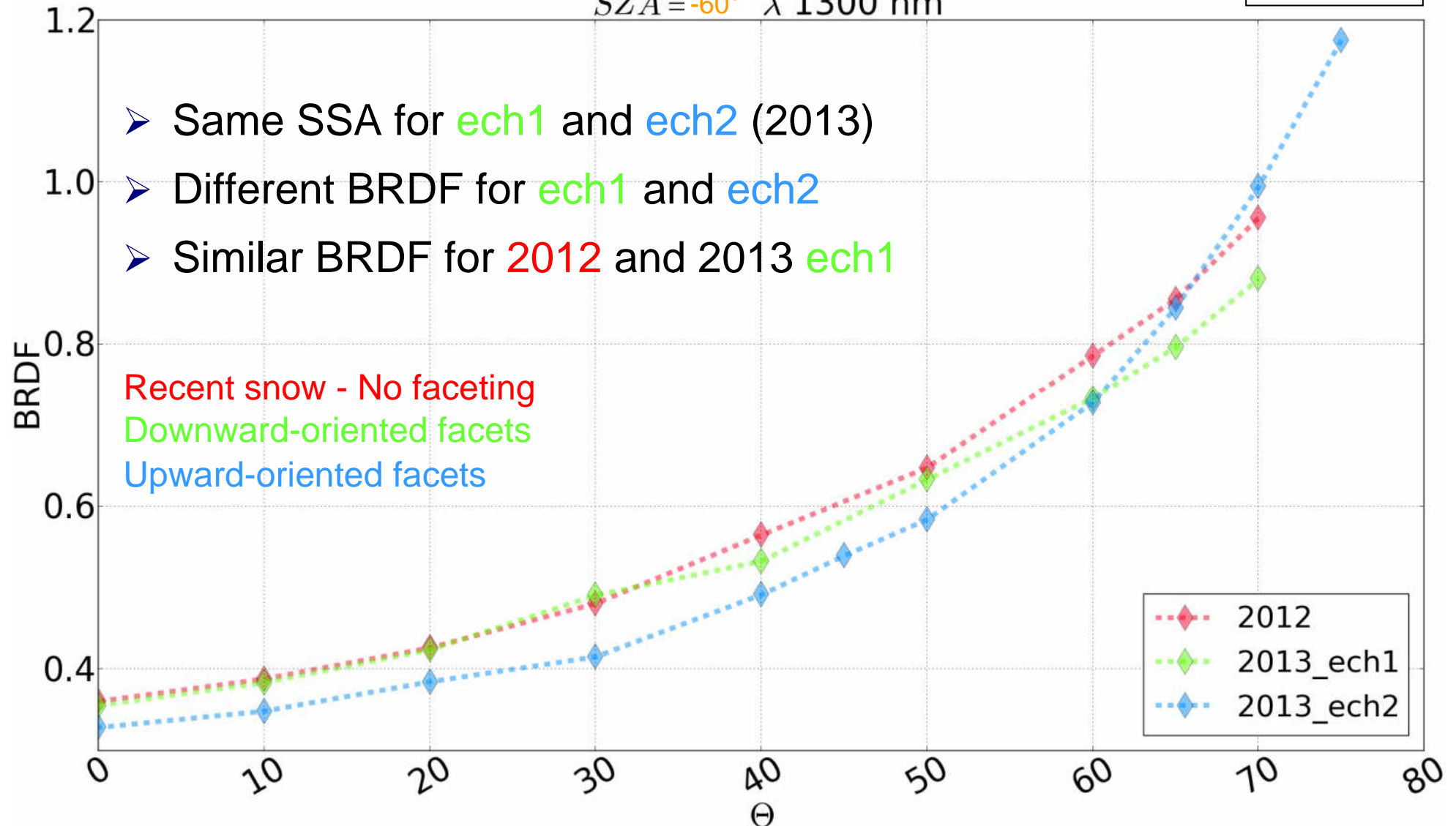
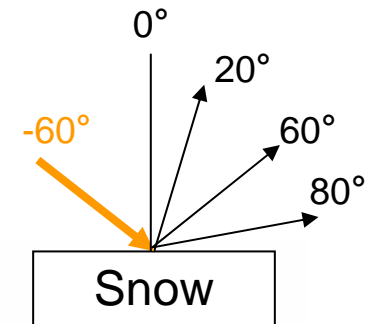




# BRDF – Impact of grain shape

Comparison mesures 2012 et 2013

$SZA = -60^\circ$   $\lambda$  1300 nm





# BRDF – Impact of grain shape

- For the same SSA but different grain shape different BRDF values were measured
- In the case of similar grain shape but different SSA values similar BRDF values were measured
- Very strong diffusion in forward direction was observed for the sample with faceted grains on the top compared to the results for rounded grains

# Conclusion and outlook

DISORT:

- Confirmation of DISORT albedo modeling for low absorbing range (900 – 1100 nm) with measurements

PBRT:

- PBRT could not be validated → strong size dependence
- Outlook:
  - Investigation of surface size and depth impact
  - Find a representative elementary volume
  - Influence of the amount of photons
  - Testing the influence of impurities



# Conclusion and outlook

Analytical model:

- Could not describe the measurements
- Adjusting the shape factor led to a better result
- Very high anisotropy of the model for the wavelength 1300 nm compared to the measurements (out of validity range)



# Conclusion and outlook

Impact of grain shape on BRDF:

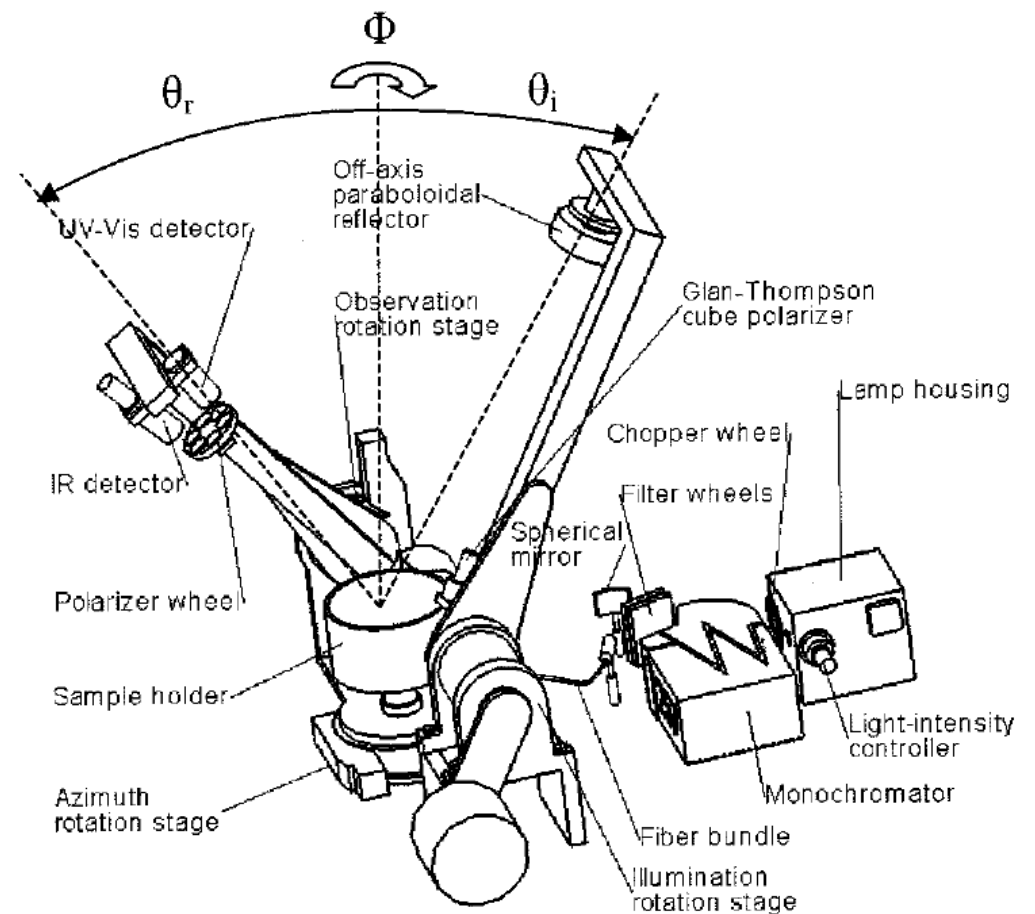
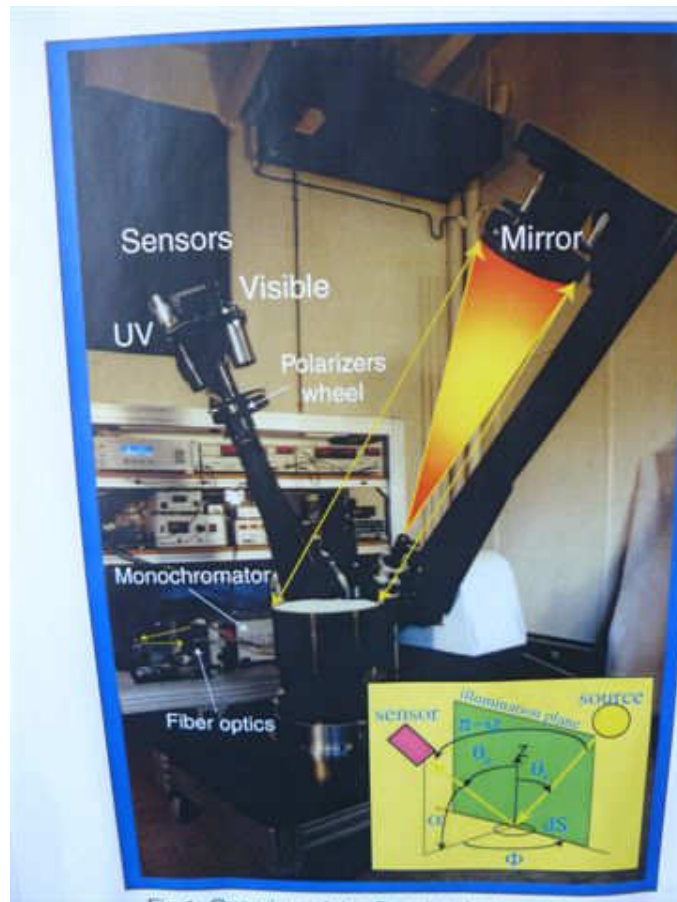
- The impact of the shape on the BRDF was found to be strong
- For the faceted snow on top a very strong forward diffusion, compared to recent snow and faceted grains oriented to the bottom, was observed.
  - could be a key to characterize the degree of metamorphism for faceted snow



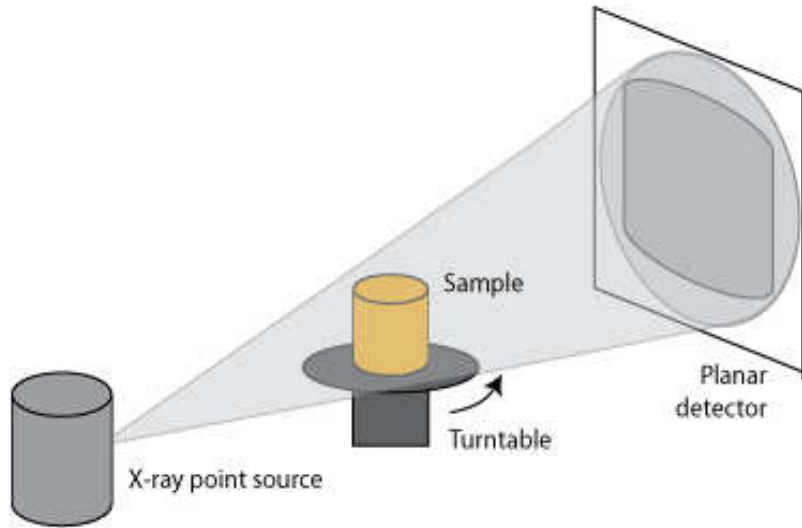
# Bibliography

- Brun, E., Martin, E., Simon, V., Gendre, C., and Coléou, C. : An energy and mass model of snow cover suitable for operational avalanche forecasting, J. Glaciol., 35, 333 – 342, 1989.
- Kaempfer, T., Hopkins, M., and Perovich, D. : A three-dimensional microstructure-based photon-tracking model of radiative transfer in snow, Journal of Geophysical Research : Atmospheres (1984–2012), 112, 2007.
- Picard, G., Brucker, L., Fily, M., Gallée, H., and Krinner, G. : Modeling time series of microwave brightness temperature in Antarctica, J. Glaciol., 55, 537 – 551, 2009.
- Haussener, S., Gergely, M., Schneebeli, M., and Steinfeld, A. : Determination of the macroscopic optical properties of snow based on exact morphology and direct pore-level heat transfer modeling, Journal of Geophysical Research : Earth Surface (2003–2012), 117, 2012.

# Spectrometer

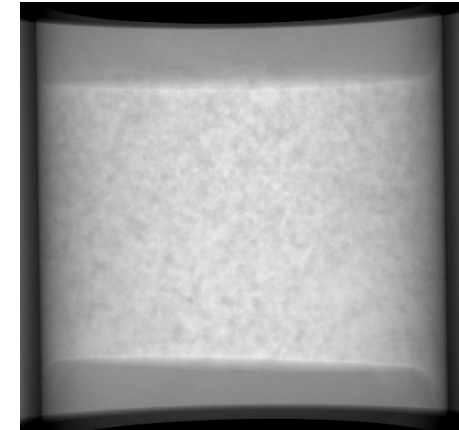
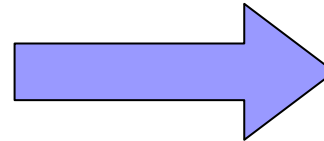


# Obtention of 3D images by X-ray tomography



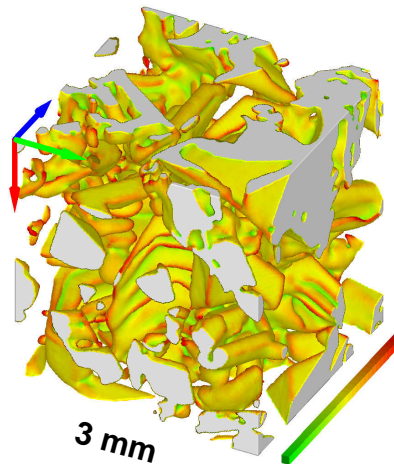
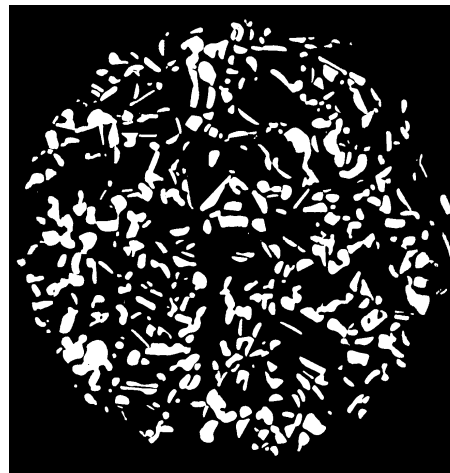
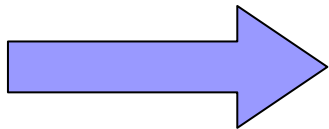
Principle of X-ray tomography

Tomography



Several radiographies of the sample at different angular positions

Thresholding and image processing



3D binary image of the sample  
→ Resolution between 7 and 9  $\mu\text{m}$

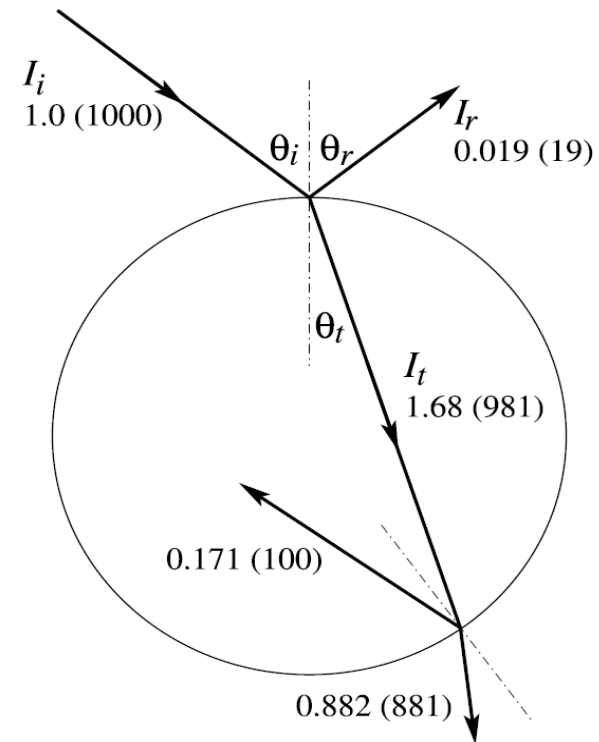


# DISORT

- Exact solution of radiative transfer equation, continuous medium
- Inputs are single scattering properties
  - Log normal distribution:
    - Logarithm of radius of spheres is normally distributed
  - Mie scattering:
    - elastic scattering of el. magnetic waves by spheres
    - size of particles in range of wavelength

# Photon tracking model PBRT

- Adapted to tomography images by R. Malgat and D. Coeurjolly (LIRIS, DigitalSnow Project)
- Interaction between ray and snow grains are governed by Snell's and Fresnel's law as well as the absorption law of Bouguer – Lambert
- Probability of reflected or transmitted photon deduced from ratio of Fresnel's law of reflected and incident radiance and a Monte-Carlo based calculation of  $\alpha$  random number between 0 and 1
- Number  $> I_r/I_i \rightarrow$  reflection
- Number  $< I_r/I_i \rightarrow$  transmission







# Analytical Model

- Based on single scattering phase function
- Takes into account directional signatures
- Valid for weakly absorbing range (ice  $< 1,24 \mu\text{m}$ )