

A Self-Stabilizing Algorithm for Edge Monitoring Problem

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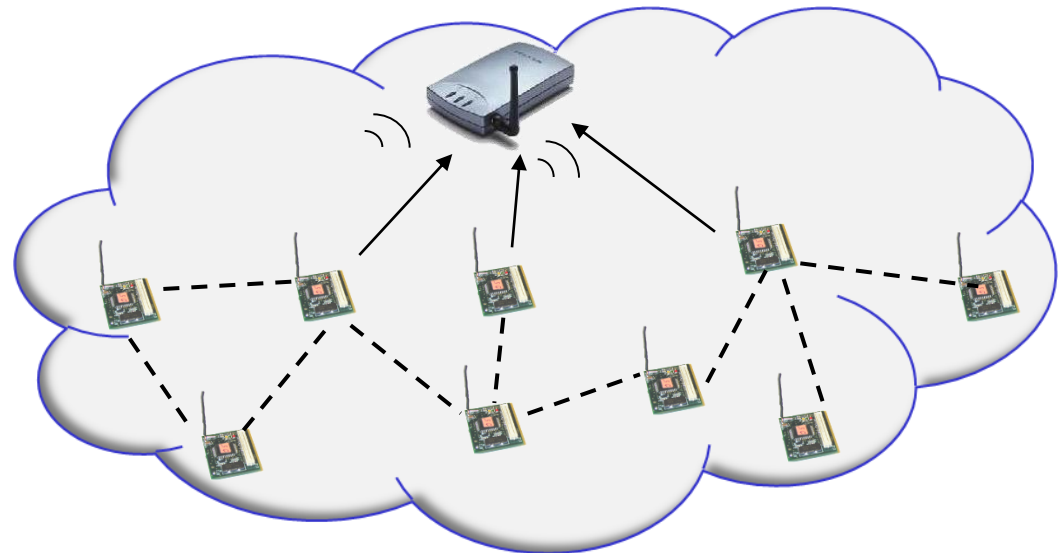
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Wireless Sensor Network (WSN)

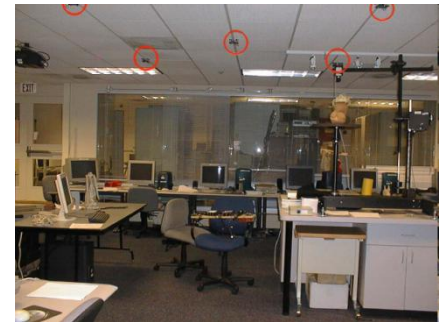
A Wireless Sensor Network (WSN) consists of distributed autonomous sensors to monitor Physical or environmental conditions such as temperature, sound, vibration, pressure.

Gateway node



WSN Applications

- Environmental/Habitat monitoring
- Acoustic detection
- Seismic Detection
- Military surveillance
- forest fire control
- Medical monitoring
- Industrial process control
- Process Monitoring
- ...

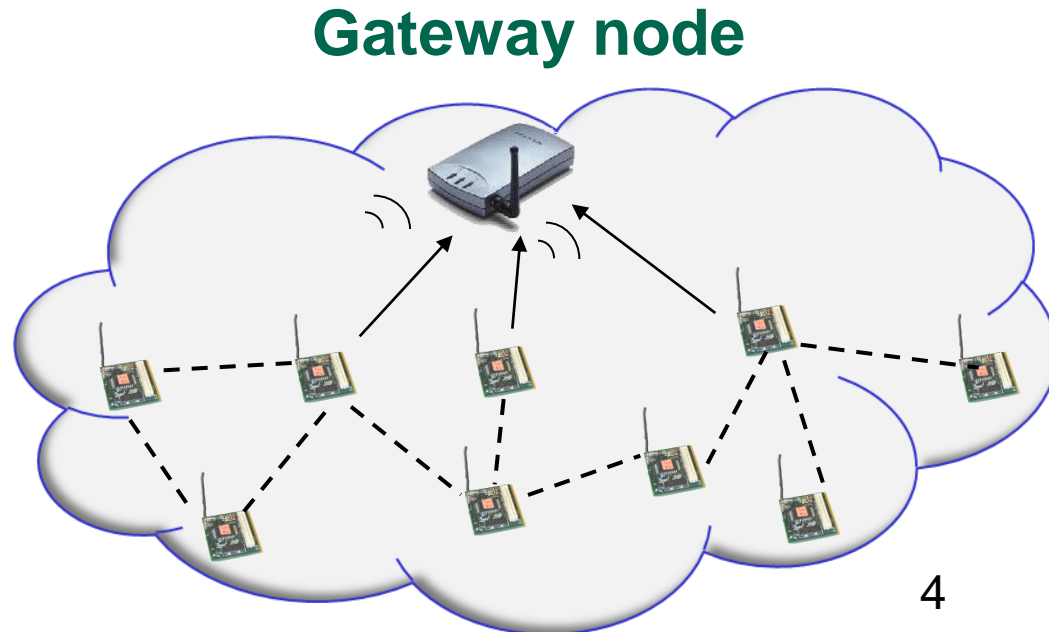


Challenges in Running a WSN

Vulnerability of WSN due to :

- Wireless communication
- Hostile unattended environments
- Limited resources of sensors

**Security of WSN
is a real challenge**



Security of WSN

Cryptography techniques are efficient for **data confidentiality and integrity**.

Are there sufficient for compromised nodes ?

NO

Security community develops **complementary** security techniques, based on the **self-monitoring**

Security of WSN

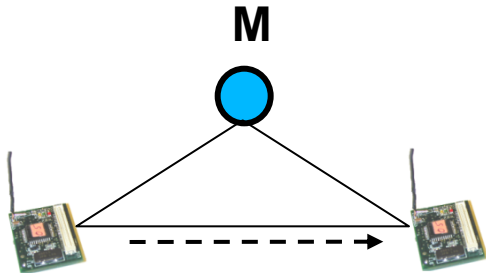
Self-monitoring : assigning monitoring roles to some of the nodes in the network.

Monitors are placed somewhere in the **intersection of the communication ranges** of the sending and the receiving nodes.

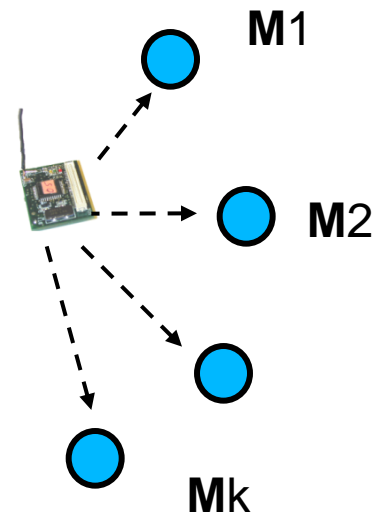
Security of WSN

We distinguish two types of self-monitoring

Edge-monitoring



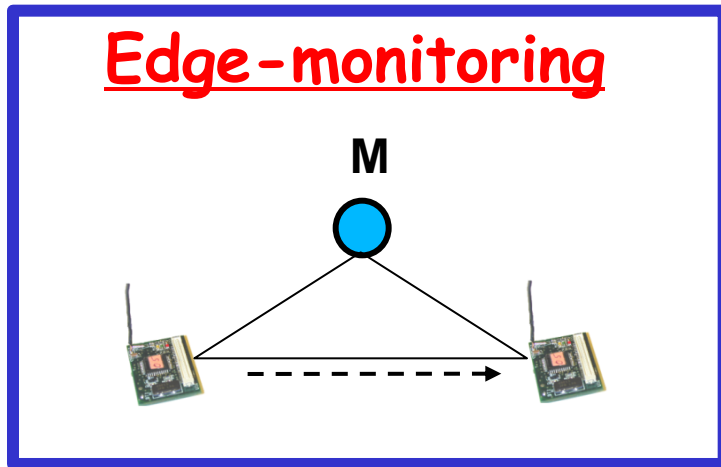
Self-protection



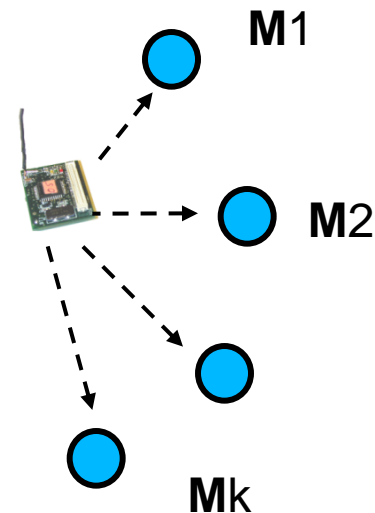
k-tuple total dominating set

Security of WSN

We distinguish two types of self-monitoring



Self-protection

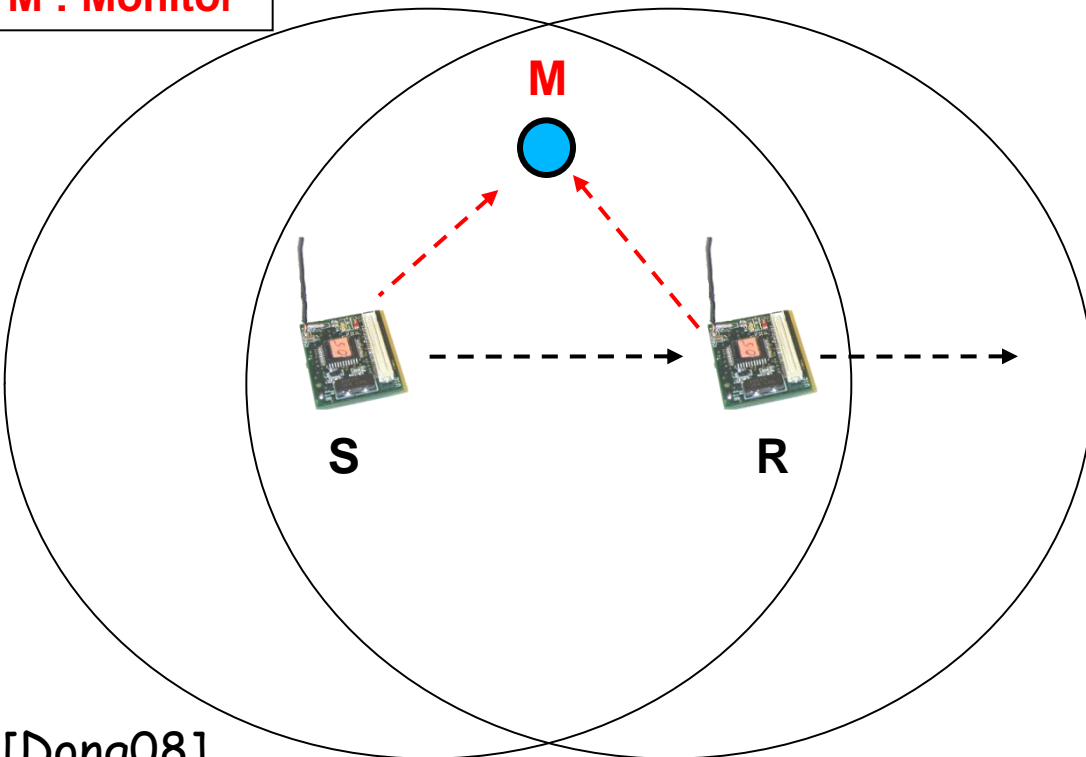


k-tuple total dominating set

Edge monitoring

This concept has been introduced in WSN by Marti et al. [Marti00]

S : Sender
R : Receiver
M : Monitor



Node M monitors link from S to R by monitoring traffic that R receives from S and forwards out

By analyzing traffic flows, monitoring nodes are able to detect behavior deviating from the specification caused by an implementation error or a fault, such as **delaying, dropping, modifying, or producing faulty packets**



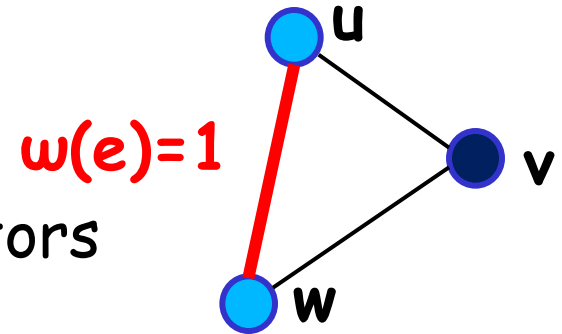
Edge monitoring

Since it is natural to model a WSN by a graph $G=(V,E)$

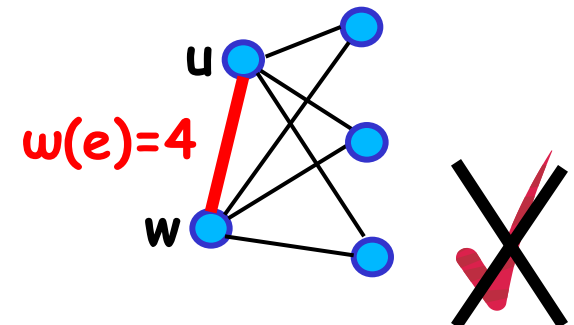
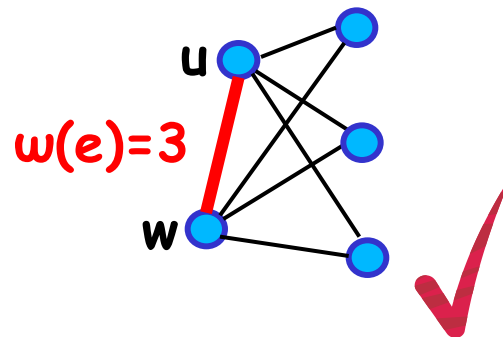
- V : set of nodes that represents the sensors
- E : set of edges that represents their communications
- We denote
 - $N(v)=\{u \in V / \langle v,u \rangle \in E\}$
 - $n=|V|$
 - $m=|E|$
 - Δ max node degree in G

Edge monitoring

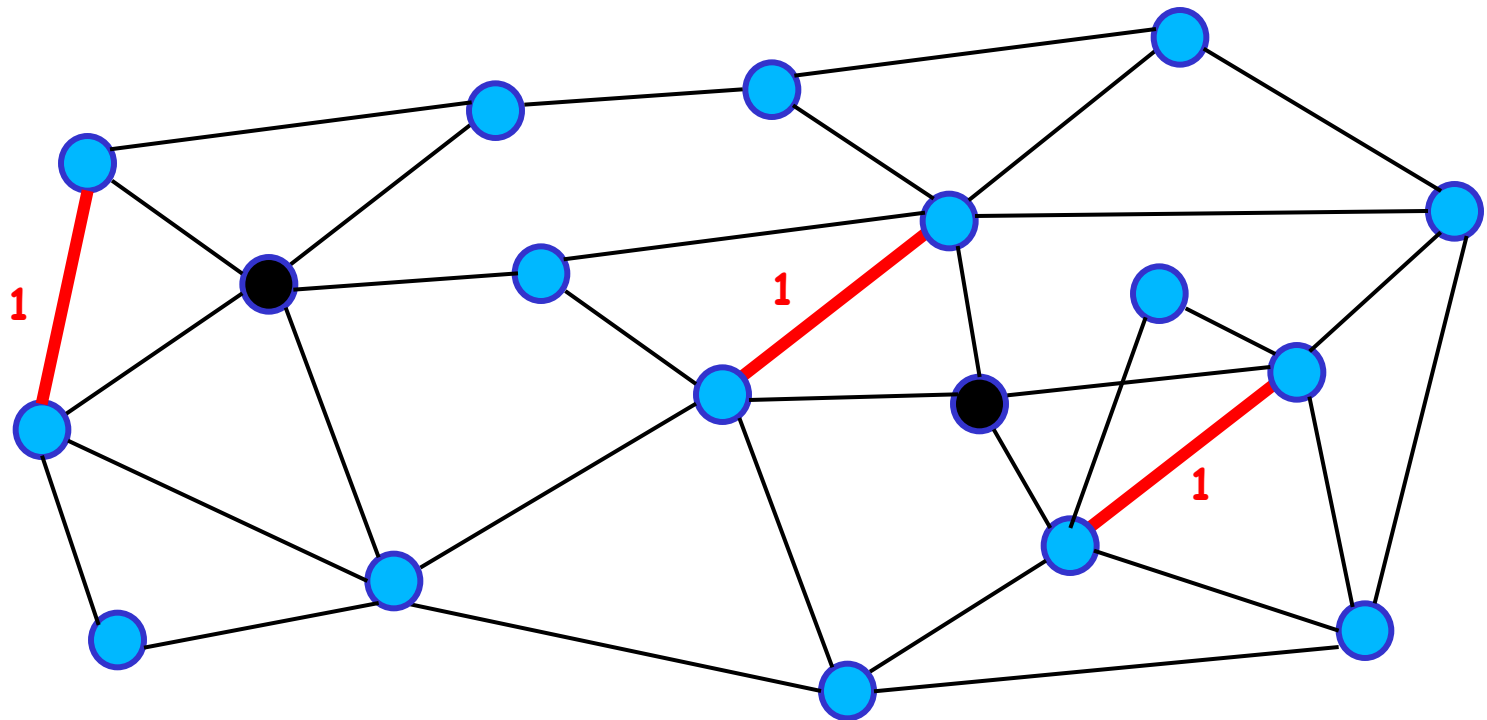
- Edges have monitoring constraints w specifying the number of required monitors



- Assumption: For each $e = \langle u, w \rangle \in E$ then $|N(u) \cap N(w)| \geq w(e)$

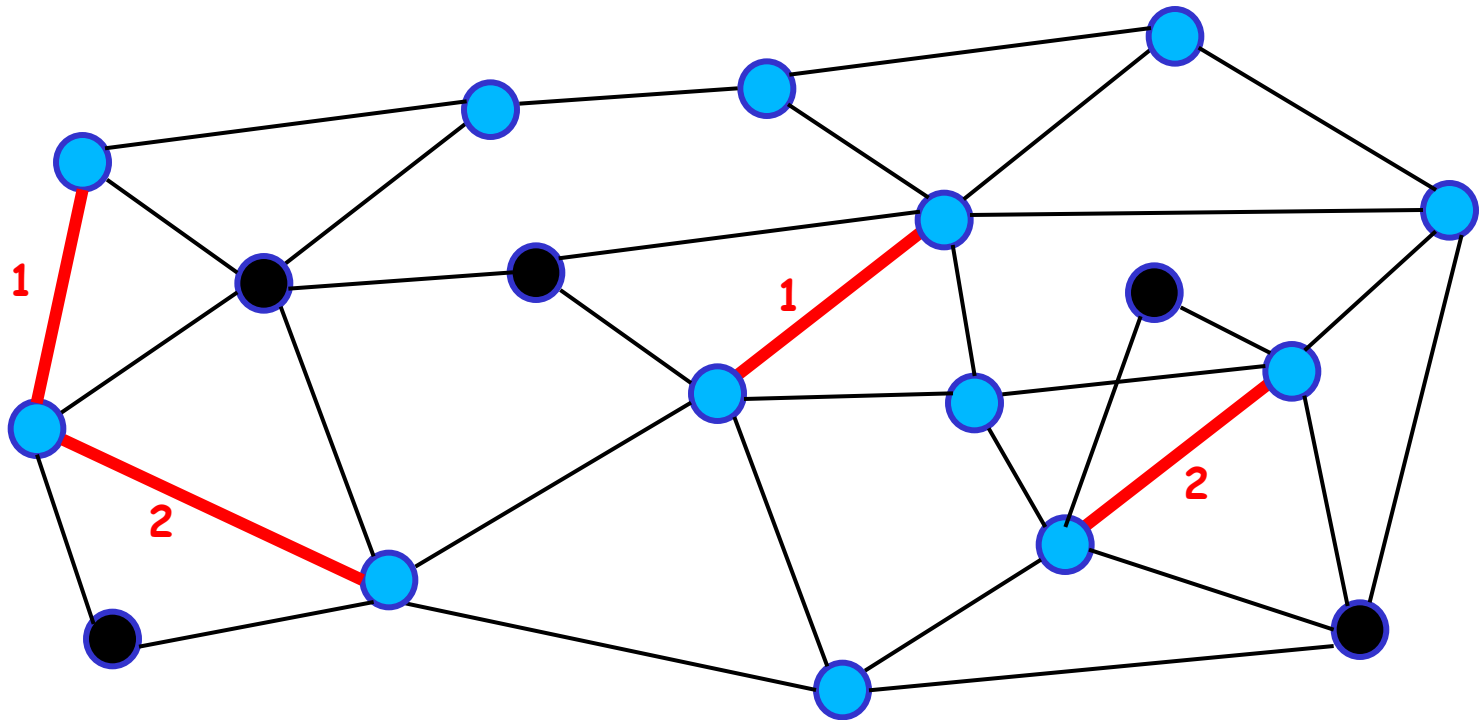


Example



red :: edges to be monitored
black :: monitors

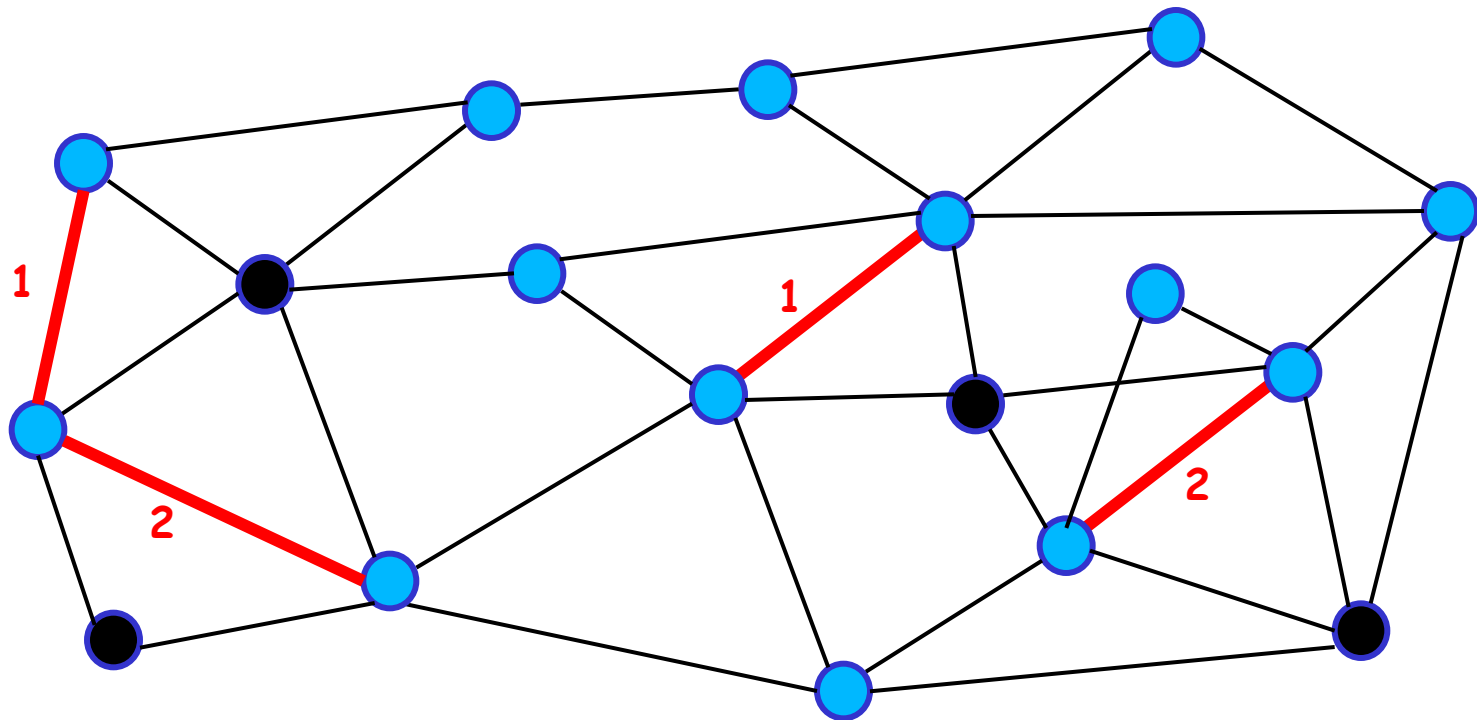
Example



red :: edges to be monitored
black :: monitors

5 monitors!

Example



red :: edges to be monitored
black :: monitors

Only 4 monitors!



Edge monitoring

- Finding a **minimum set** of edge monitoring nodes is NP-hard
- **Goal:** Minimal edge monitoring sets
 - i.e. a subset D of nodes s.t. for each edge $e \in E$ there are at least $w(e)$ nodes in D that can monitor e and no proper subset of D satisfies this property
- Distributed algorithms with provable approximation ratios are known [Dong08, Dong11]
- What about self-stabilizing algorithms?



Previous Work

- Hauck proposed the first self-stabilizing algorithm for minimal edge monitoring problem [Hauck12]
- $O(n^2m)$ moves under unfair distributed scheduler

Reference	Dist. knowledge	Transformer	Com. model	Self-stab. ?	Complexity.
[Dong 08] [Dong 11]	Distance-two	Yes	Synchronous	No	$O(\Delta)$
[Hauck 12]	Expression model	Yes	Asynchronous	Yes	$O(n^2 m)$
Our paper	-	-	-	-	-



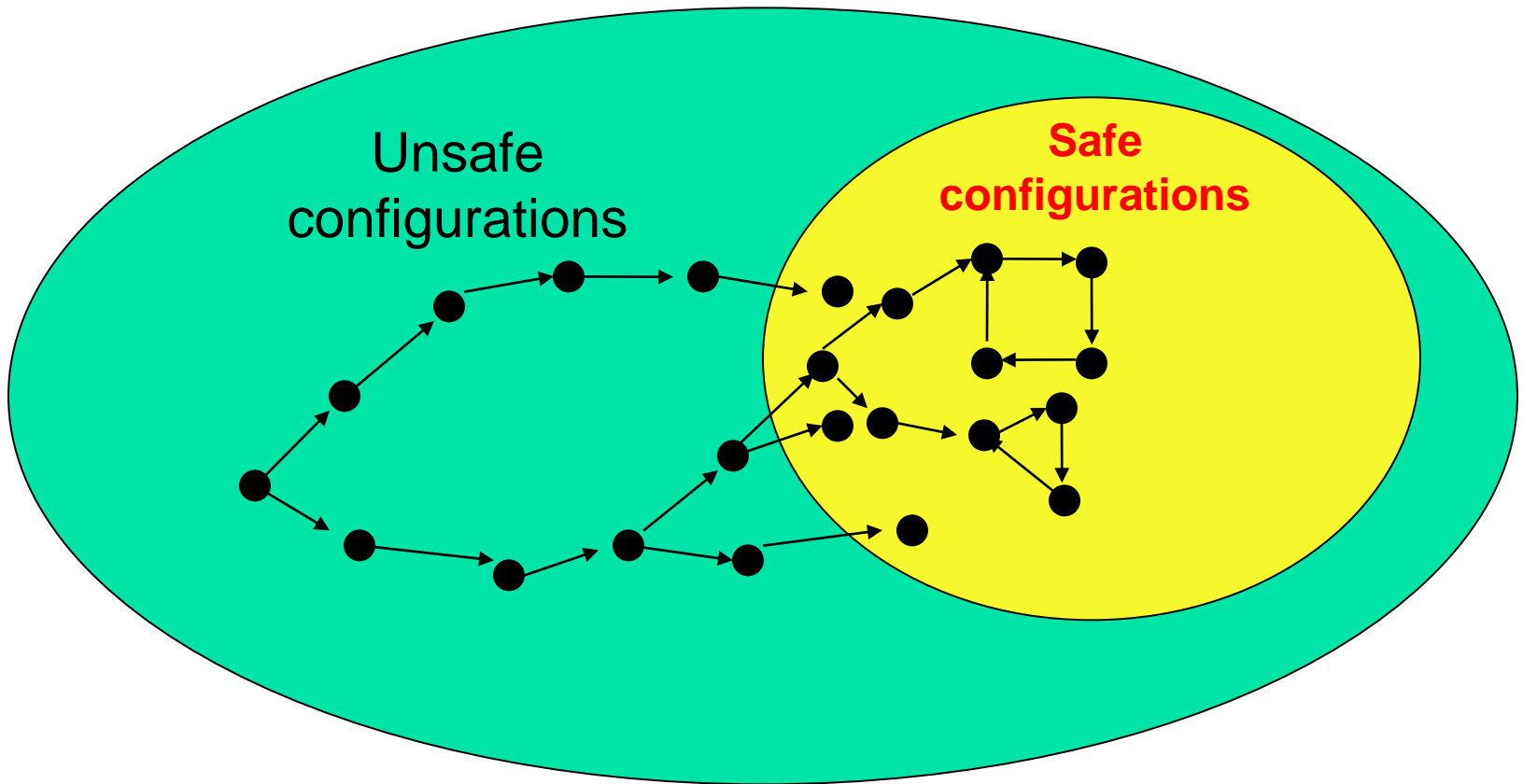
Contribution

New self-stabilizing algorithm for computing minimal edge monitoring set: SEMS

Algorithm SEMS operates under the unfair distributed scheduler and converges in $O(\Delta^2 m)$ moves

Reference	Dist. knowledge	Transformer	Com. model	Self-stab. ?	Complexity.
[Dong 08] [Dong 11]	Distance-two	Yes	Synchronous	No	$O(\Delta)$
[Hauck 12]	Expression model	Yes	Asynchronous	Yes	$O(n^2 m)$
Our paper	Distance-one	No	Asynchronous	Yes	$O(\Delta^2 m)$

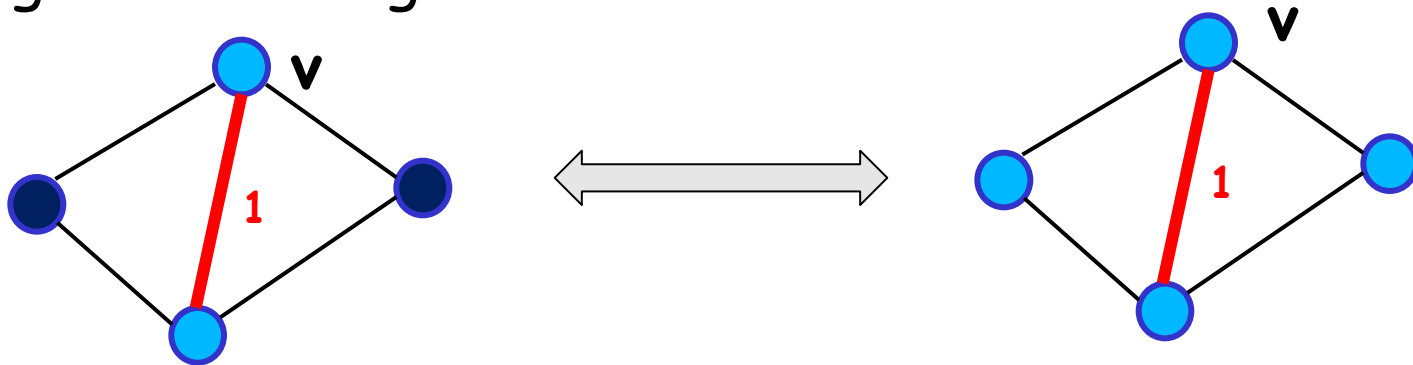
Self-stabilizing algorithm



- Self-Stabilization = Closure + Convergence

Algorithm for minimal Edge monitoring set (SEMS)

- Edge Monitoring



- **Problem:** Critical nodes are not neighbors
- **Solution:** Intermediate nodes give permission to a single neighbor to make a move
- **Problem:** Deadlocks may arise
- **Solution:** Enforce ordering (based on *ids*)

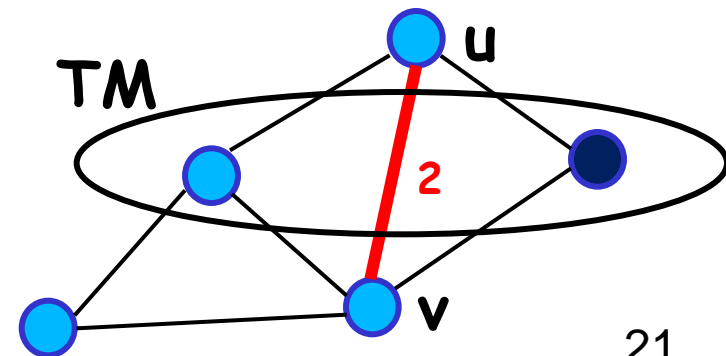


SEMS

- Each node maintains a variable state with range $\{IN, OUT, WAIT\}$
- Nodes with state **IN** are **monitors**
- State **WAIT** is an **intermediate state** from **IN** to **OUT** required for symmetry breaking

SEMS

- Monitors of an edge are **administered** by end node of edge with **smaller identifier**
- Neighbors of v that do or could monitor an edge adjacent to v are called **target monitors**
- A node maintains for each edge it is responsible for a set of target monitors (TM)

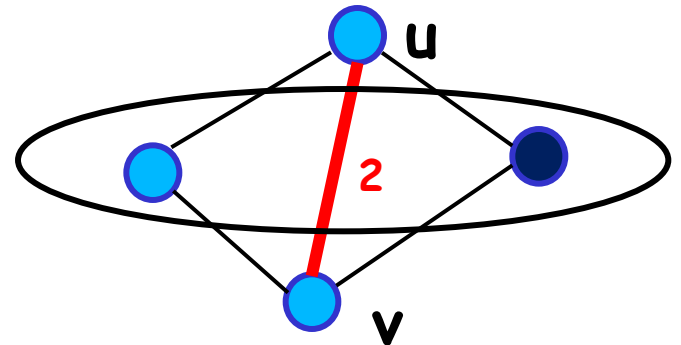


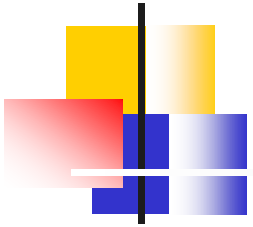
SEMS

Rule to maintain TM of edge $e = (v,u)$

1. If number of common neighbors of v and u with state IN or WAIT is larger than $w(e)$ then let $TM = \emptyset$

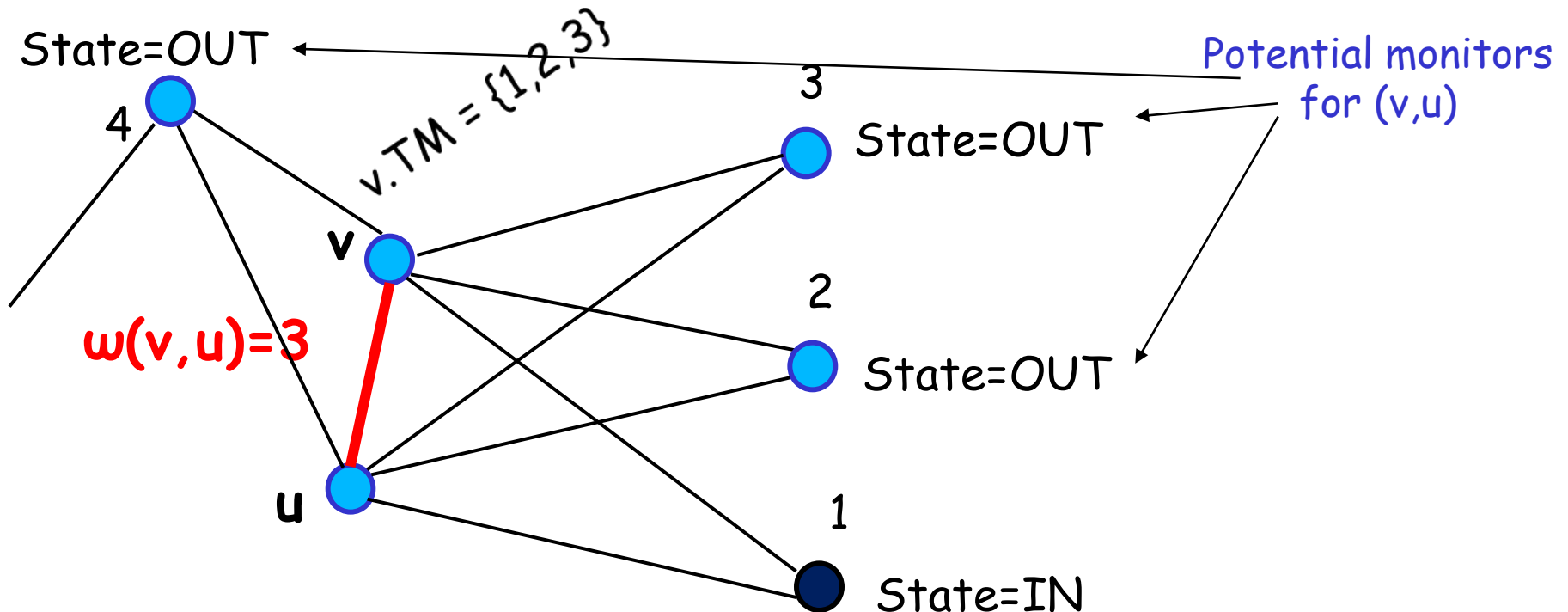
2. Otherwise TM consists of common neighbors of v and u with state IN or WAIT. If this number is less than $w(e)$ then smallest common OUT neighbors are added

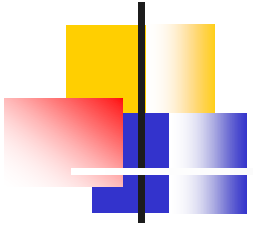




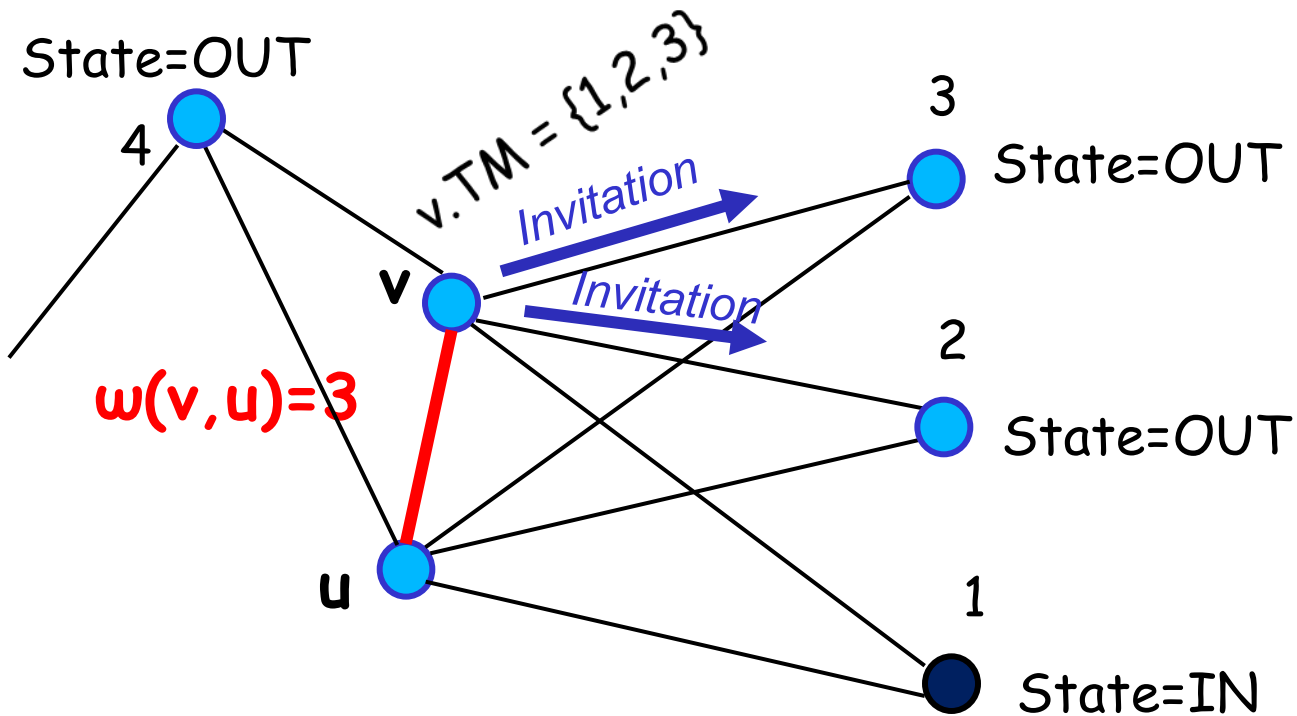
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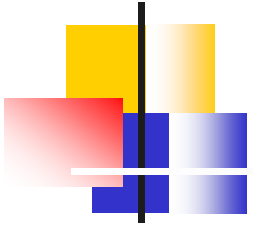
If an OUT node discovers that it is contained in TM of a neighbor it regards this as an invitation to change to IN



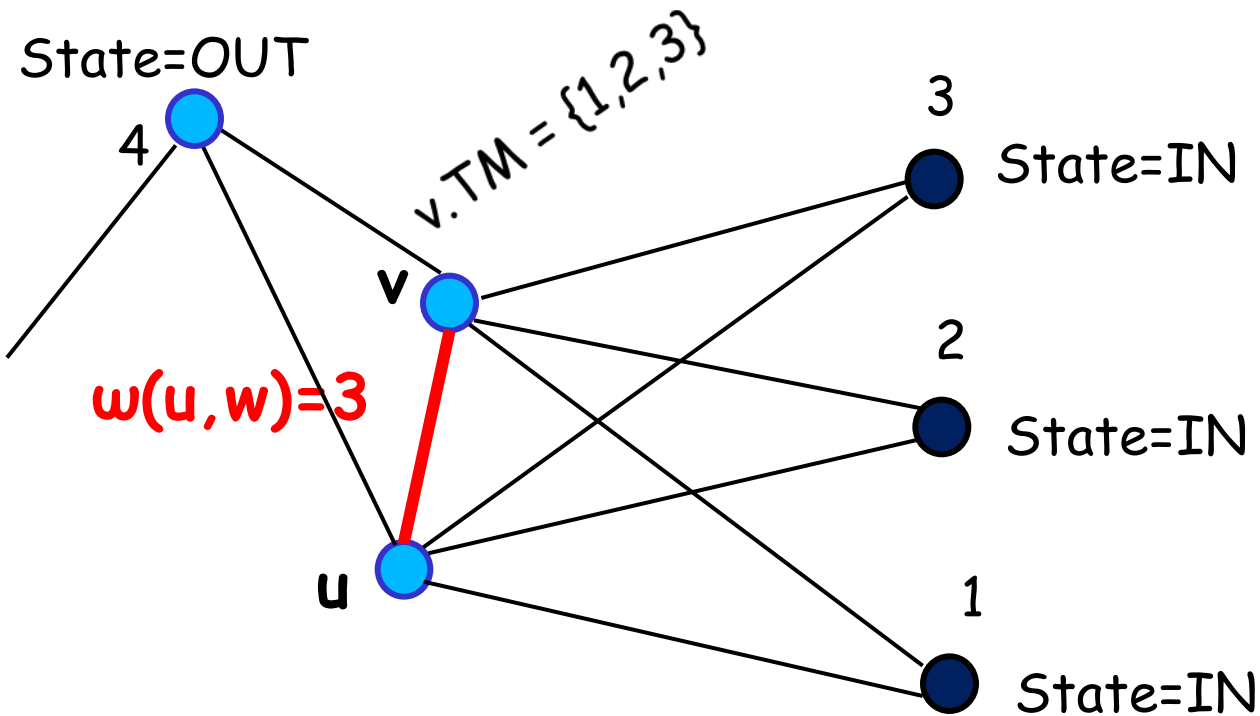


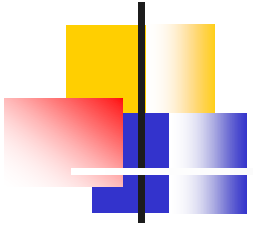
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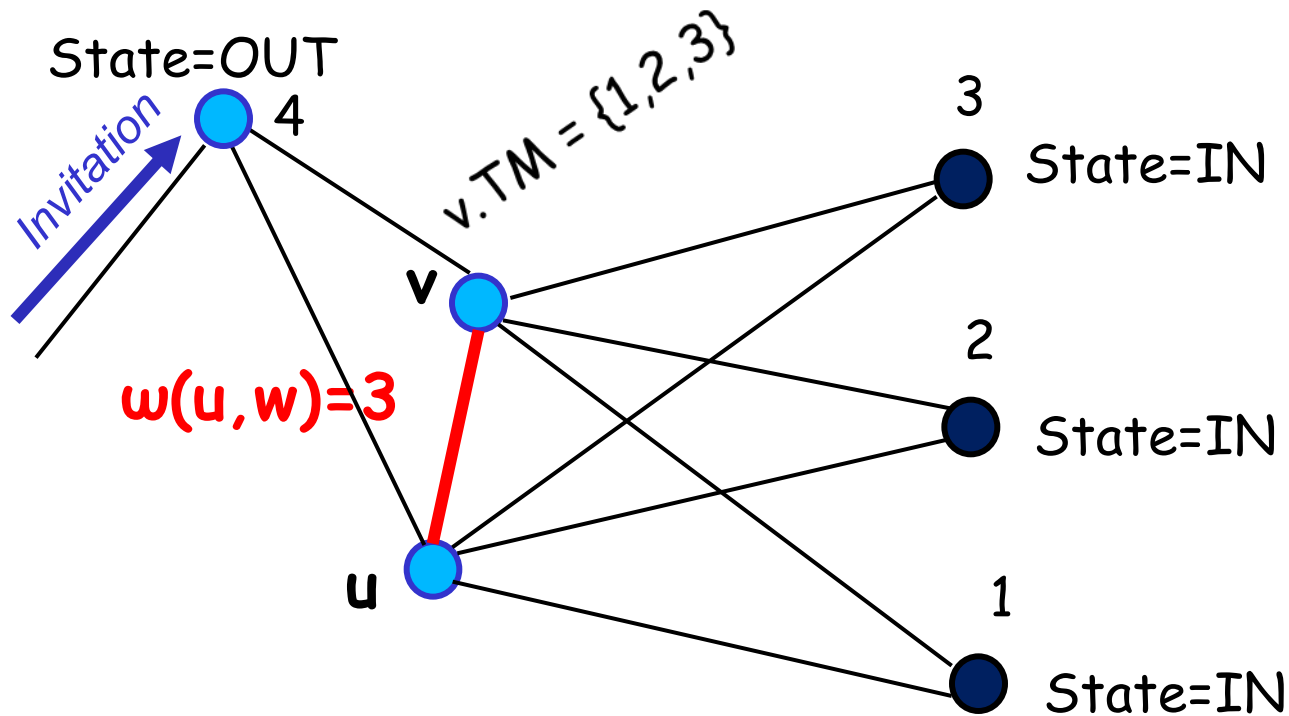


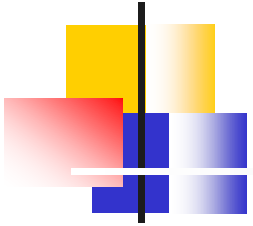
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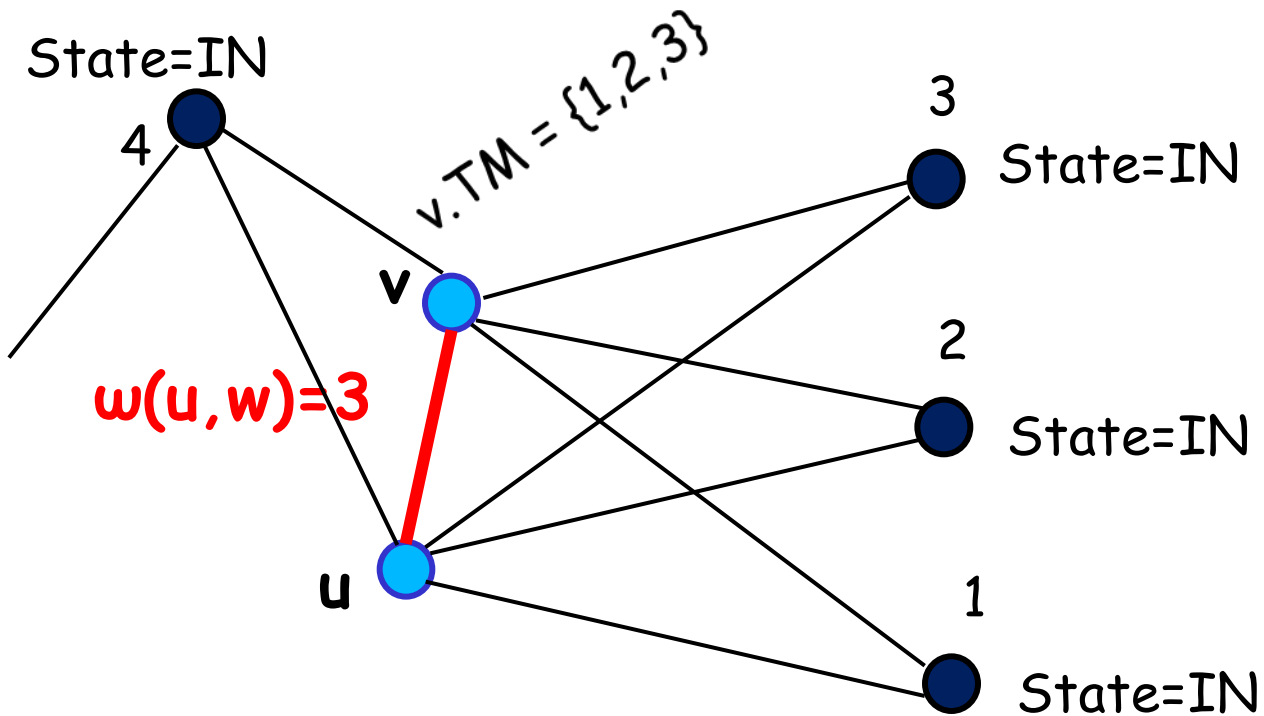


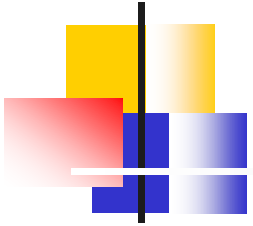
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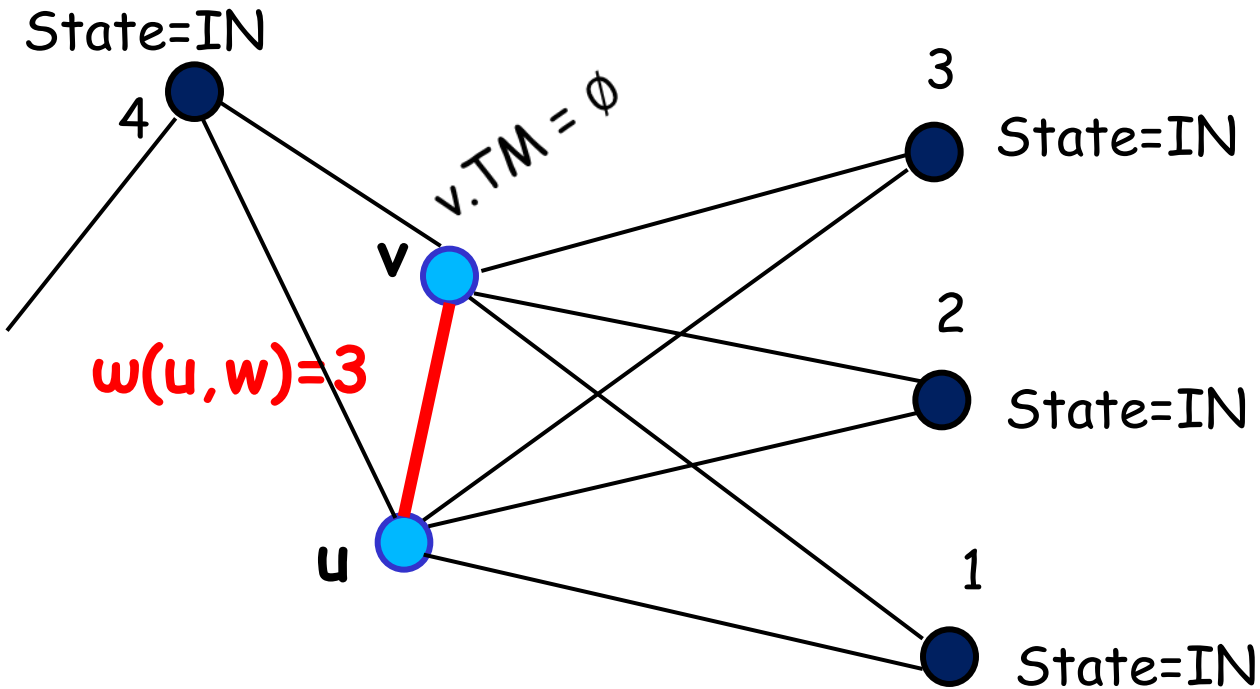


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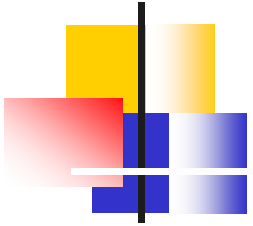
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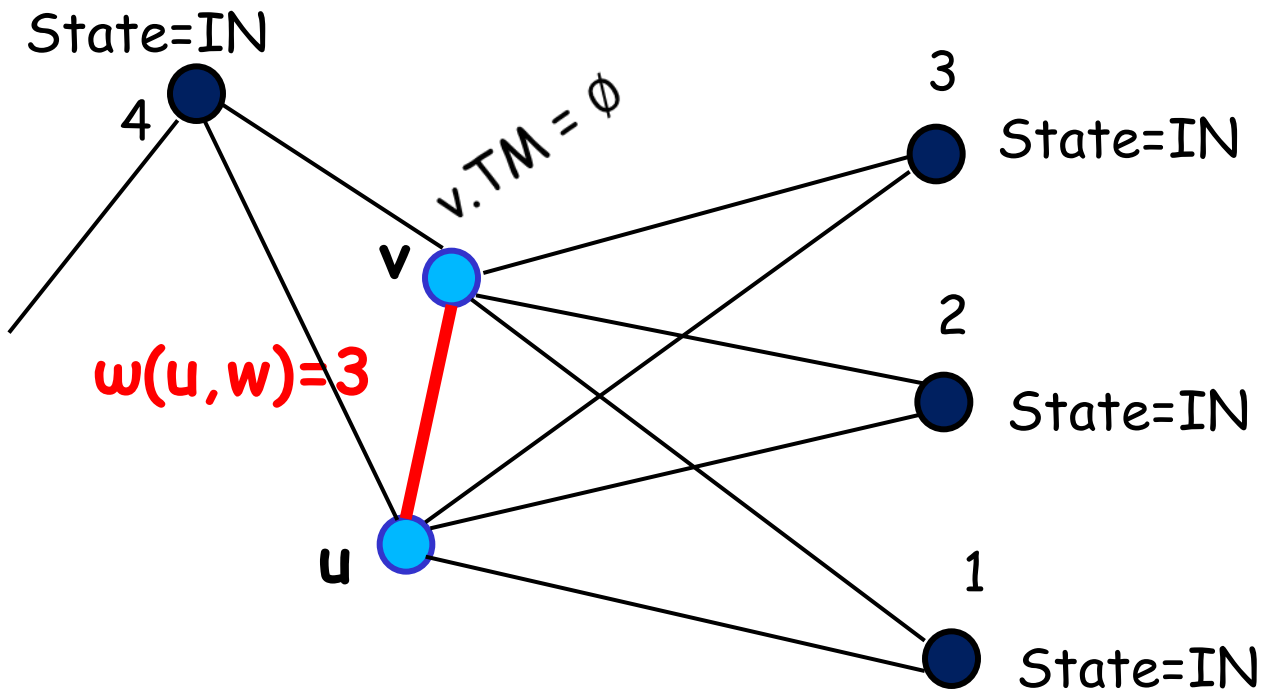


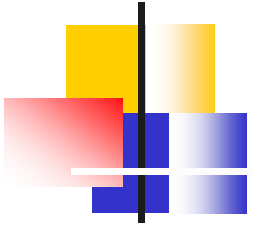
SEMS

- Nodes with state IN that are not target monitor for any neighbor changes from IN to WAIT
- To transit from WAIT to OUT, all neighbors must give permission
- A node gives this permission (variable PO) to neighbor with state WAIT with smallest identifier

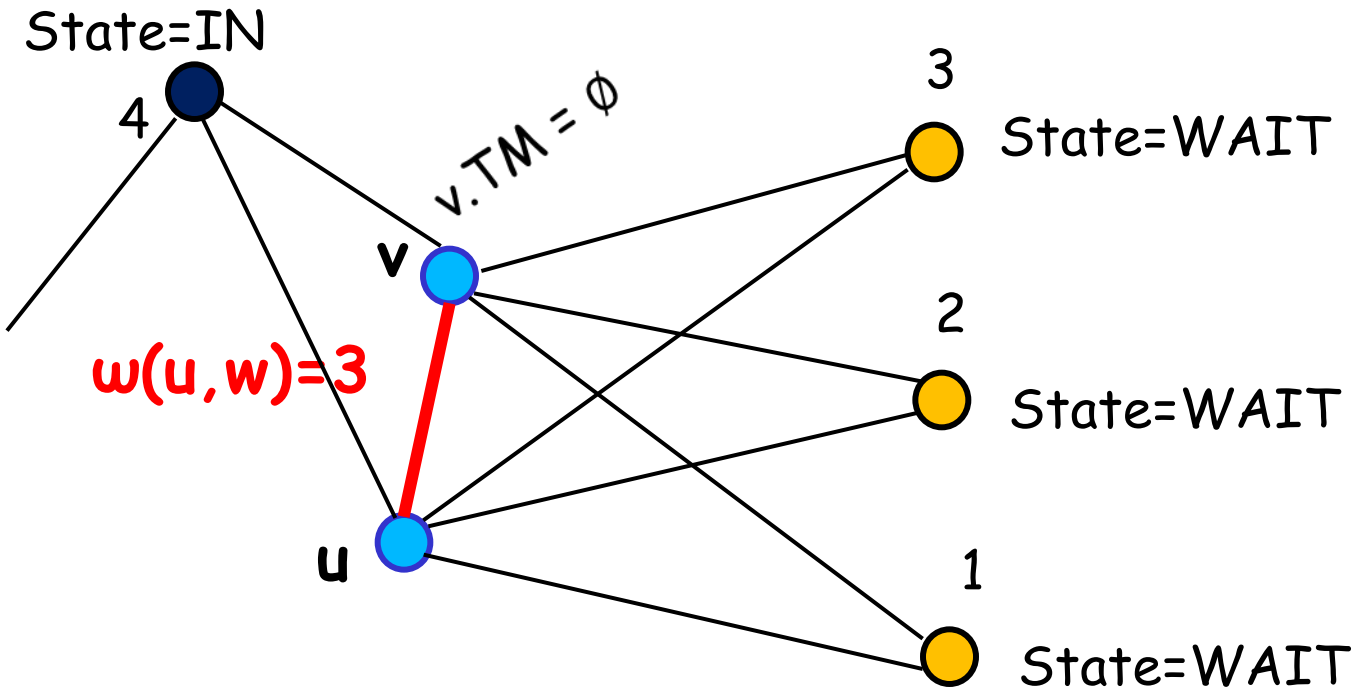


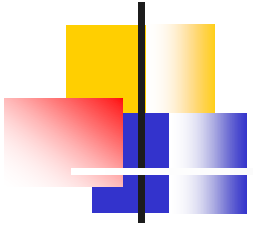
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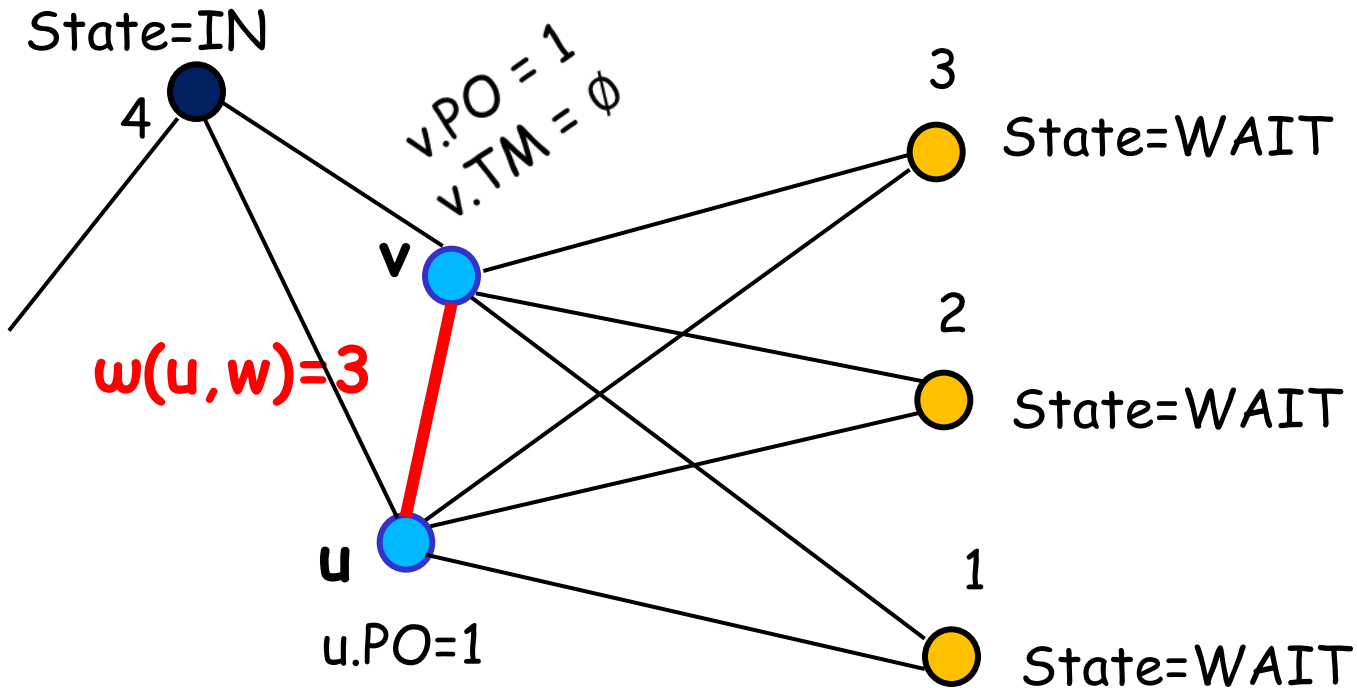


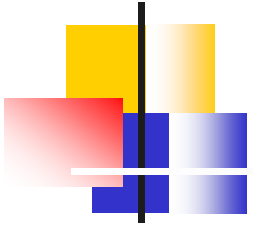
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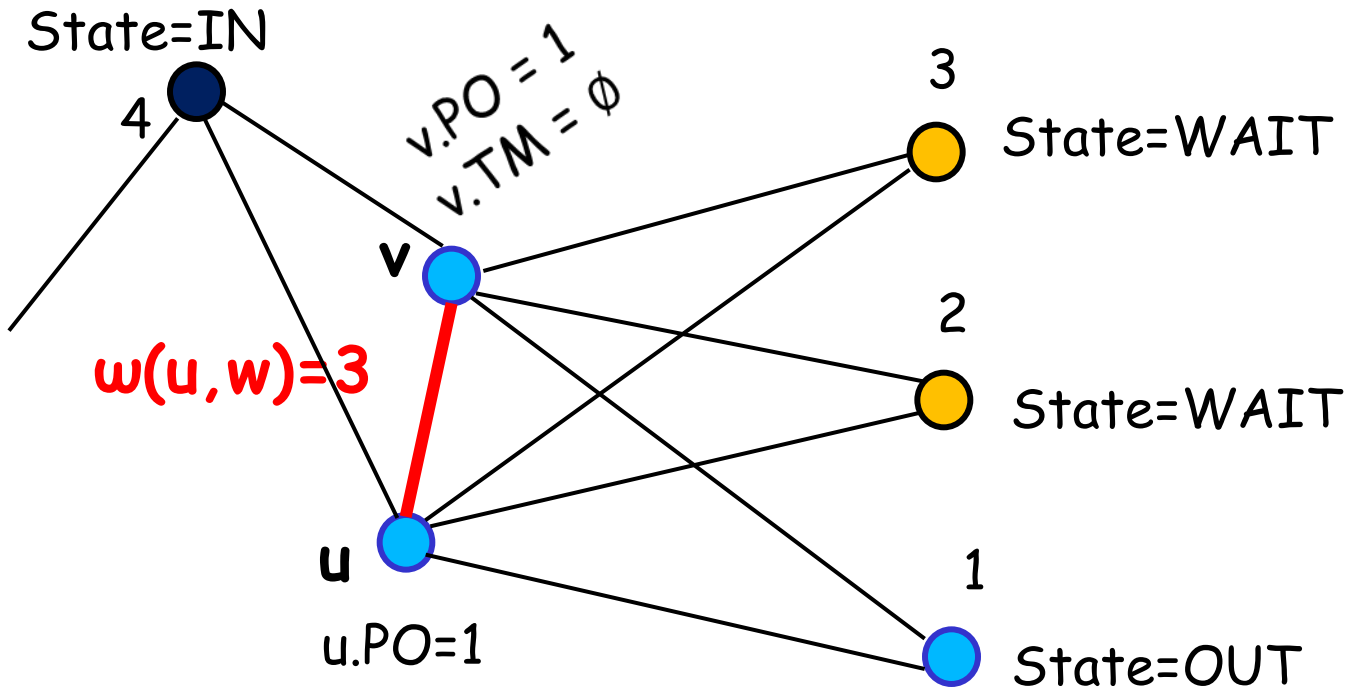


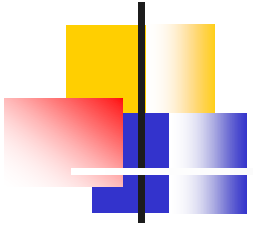
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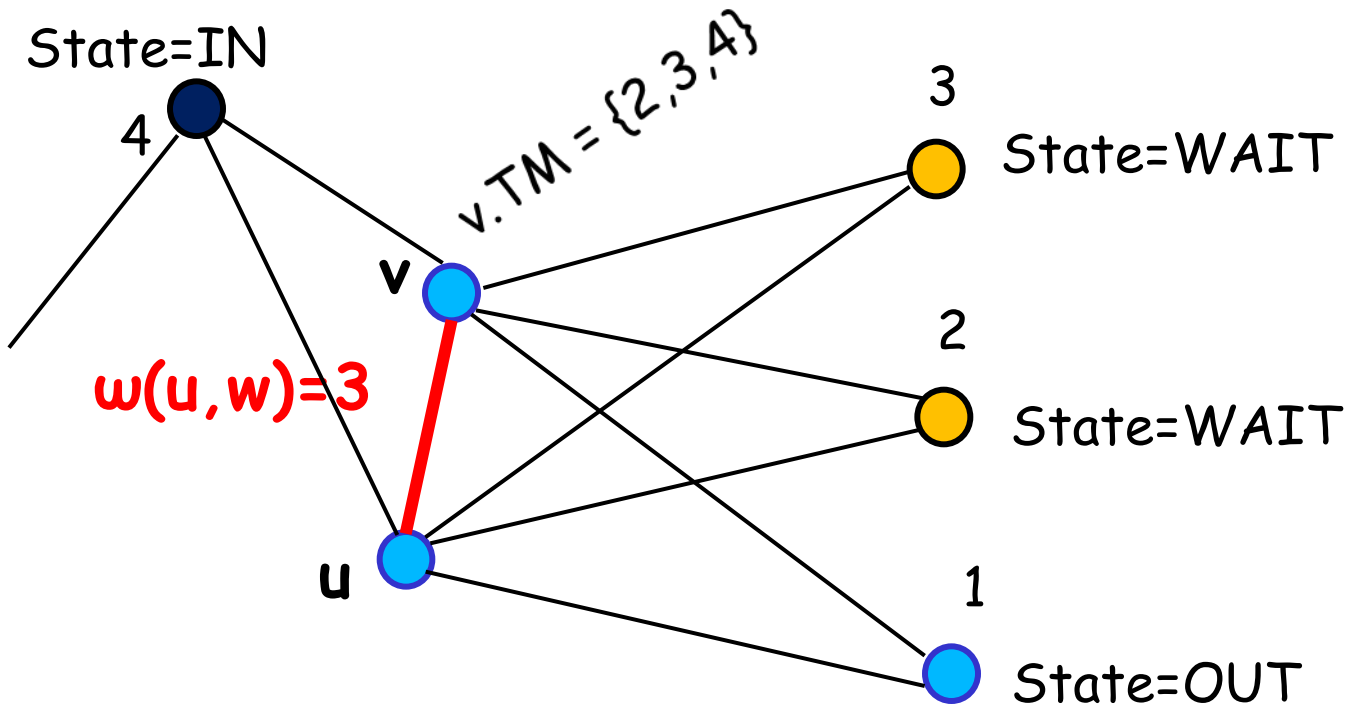


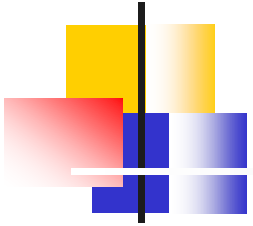
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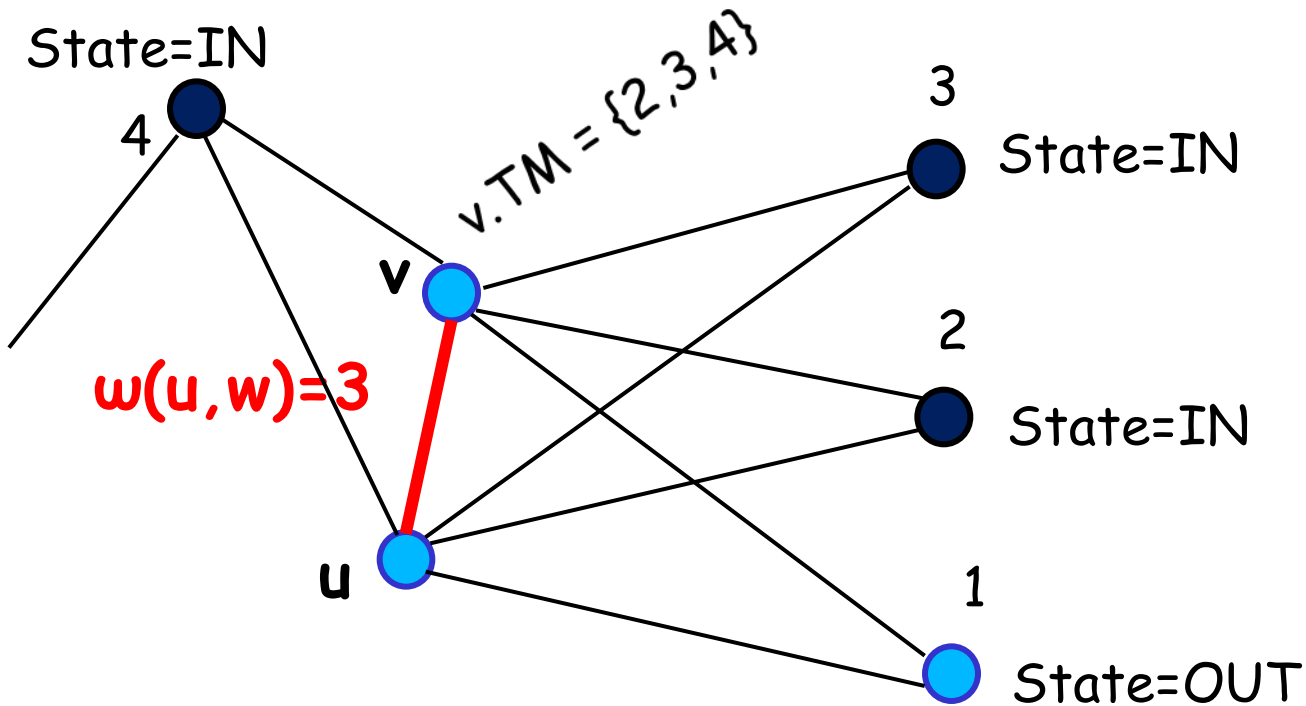


SEMS





SEMS





SEMS

Variables for each node v :

- **TM** :: the set of target monitors (note that $|TM| \leq \Delta$)
- **PO** :: contains the smallest id of all neighbors in state WAIT not contained in TM or null - used to give permission to change state to OUT



SEMS: Formal Definition

Two groups of rules:

- Management of invitations and permissions
- Management of state

Algorithm *SEMS*: Maintaining *TM*, *PO* and *S*

Nodes: v is the current node

$S \neq N(v) \longrightarrow S := N(v);$ [R1]

$TM \neq \bigcup_{u \in N(v)} TM_e(v, u) \vee PO \neq \min\{u \in N(v) \mid u.state = Wait \wedge u \notin TM\}$

$\longrightarrow TM := \bigcup_{u \in N(v)} TM_e(v, u);$

$PO := \min\{u \in N(v) \mid u.state = Wait \wedge u \notin TM\};$ [R2]



SEMS: Formal Definition

Algorithm *SEMS*: Maintaining *state*

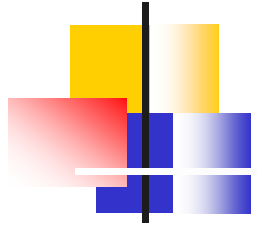
Nodes: v is the current node

$state = Out \wedge \exists u \in N(v) : v \in u.TM \wedge \forall w \in N(v) : v \neq w.PO$
 $\longrightarrow state := In;$ [R3]

$state = In \wedge \forall u \in N(v) : v \notin u.TM$ $\longrightarrow state := Wait;$ [R4]

$state = Wait \wedge \exists u \in N(v) : v \in u.TM$ $\longrightarrow state := In;$ [R5]

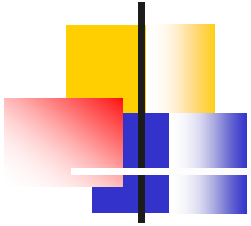
$state = Wait \wedge \forall u \in N(v) : v = u.PO$ $\longrightarrow state := Out;$ [R6]



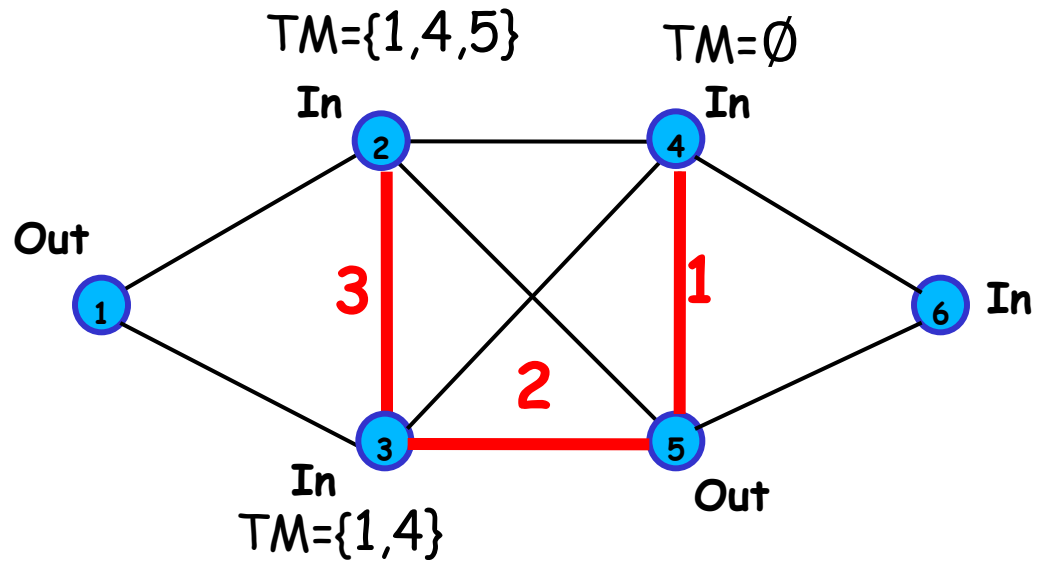
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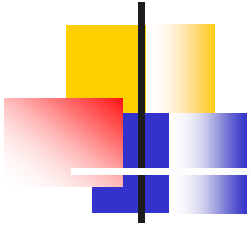
Example with corrupted state

To simplify the example, we consider the synchronous scheduler

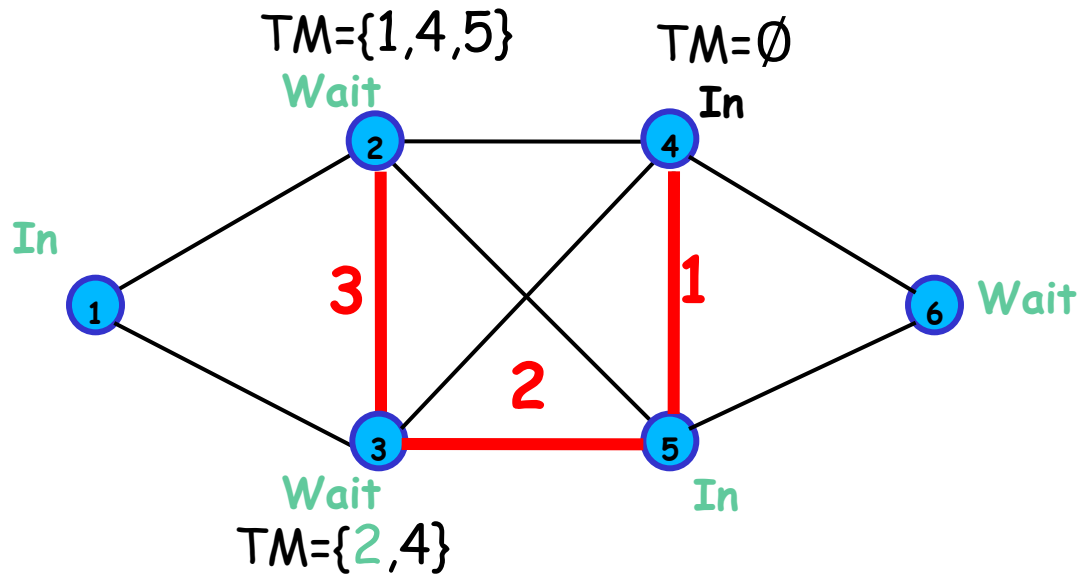


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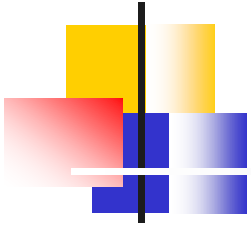




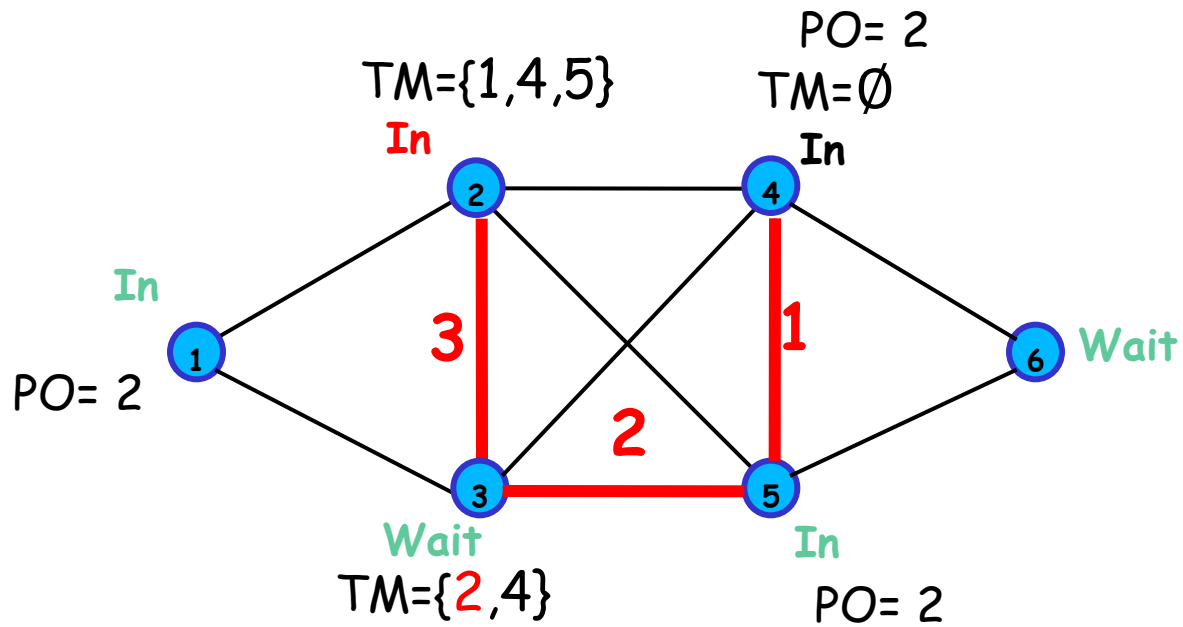
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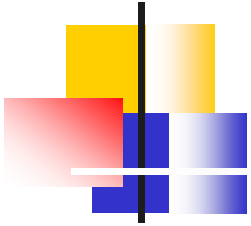
Step 1



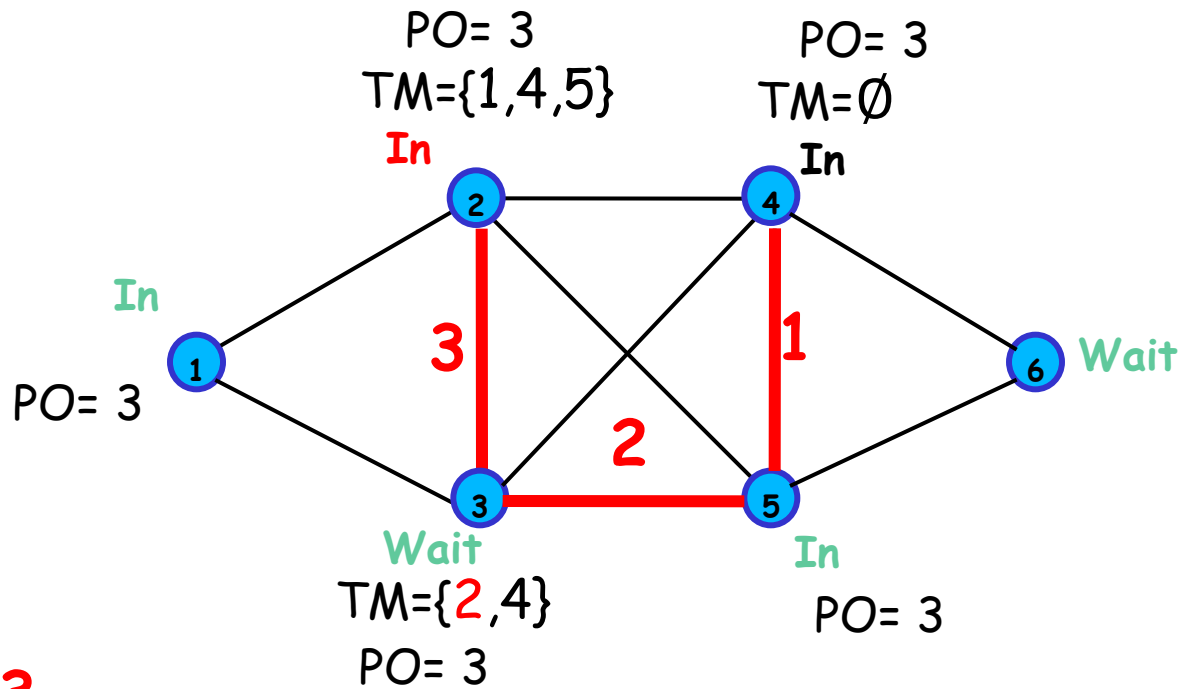
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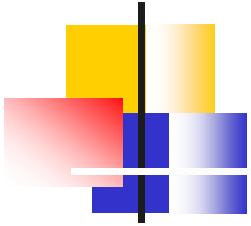
Step 2



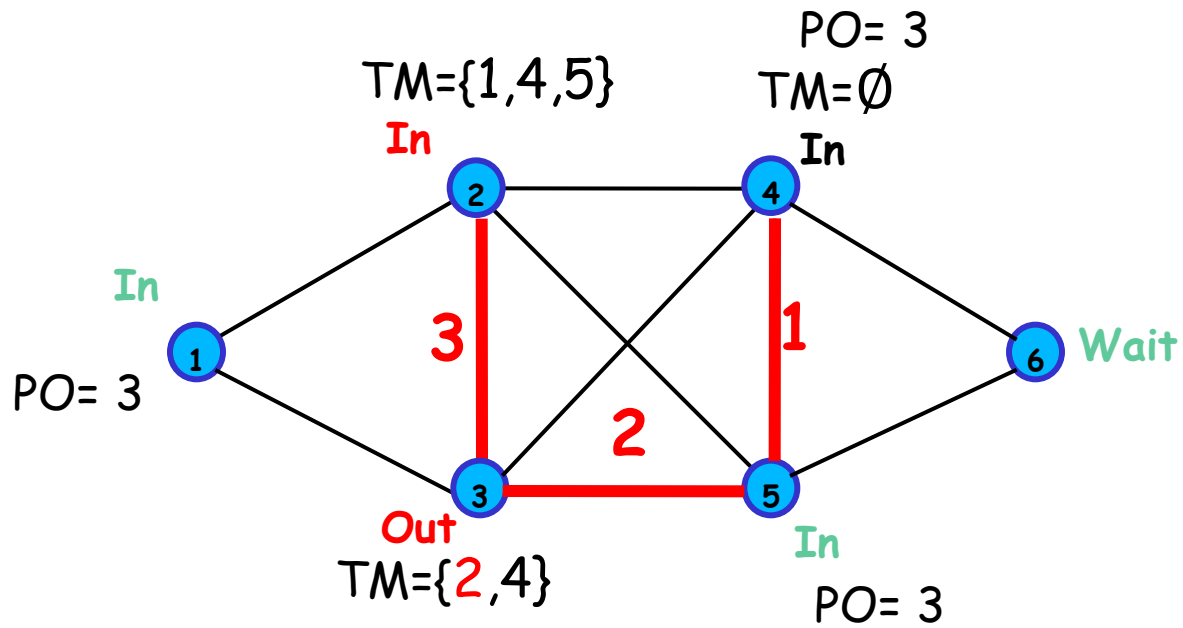
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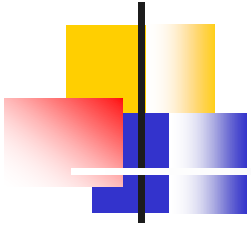
Step 3



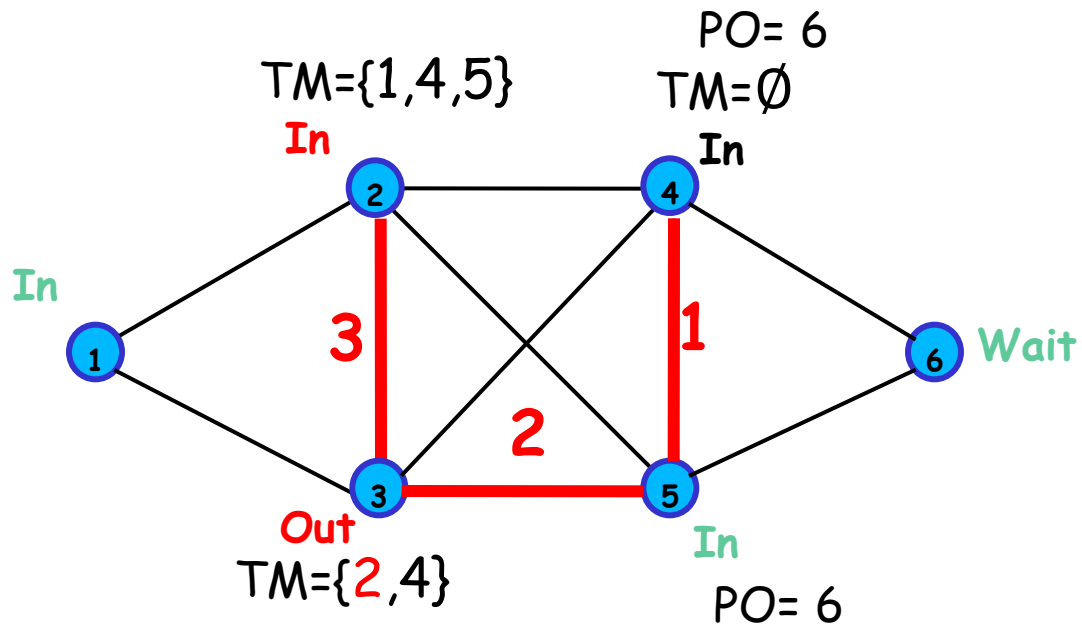
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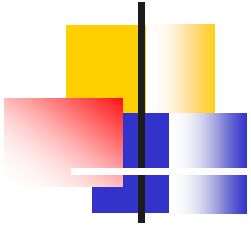
Step 4



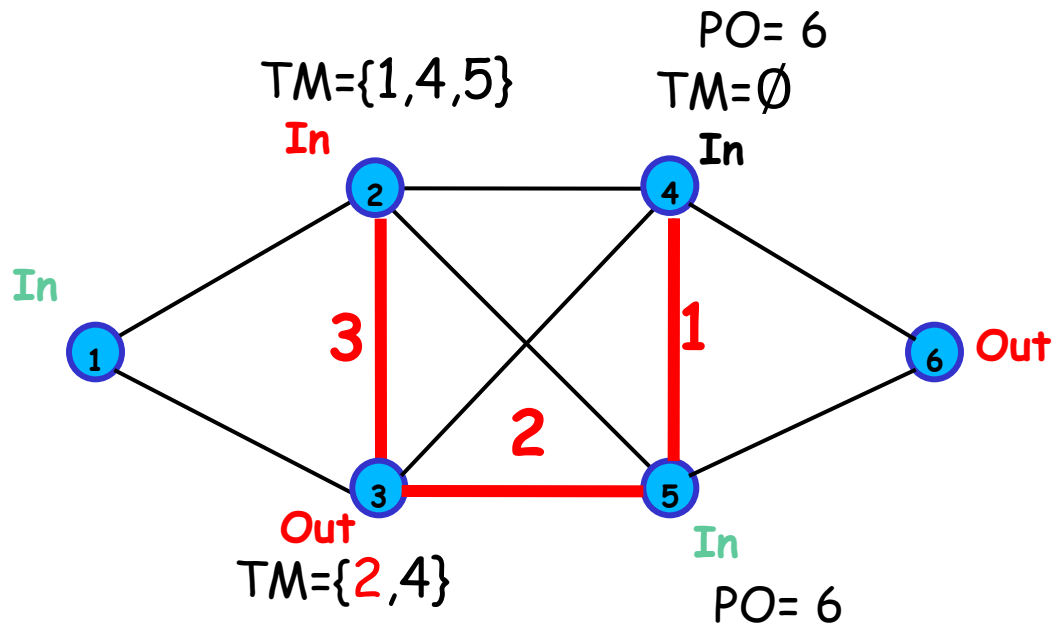
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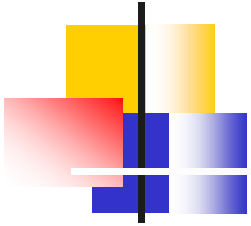
Step 5



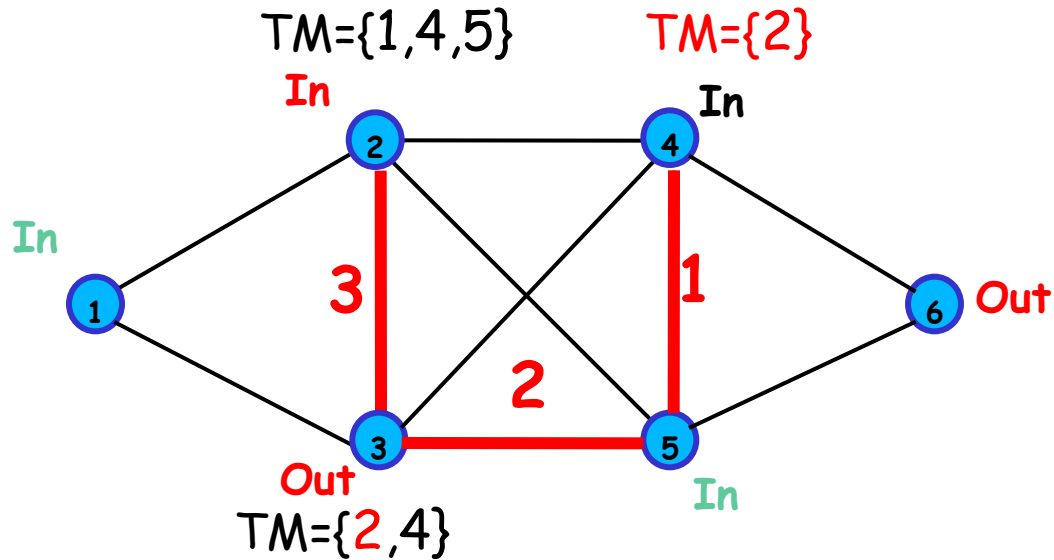
SEMS



Step 6



SEMS



Step 7

Final configuration



Conclusions & future work

Contribution:

- SEMS: A self-stabilizing algorithm for computing a minimal edge monitoring set
- SEMS converges in $O(\Delta^2 m)$ moves under unfair distributed scheduler
- Improving on previous work (Hauck $O(n^2 m)$ moves)
- No transformer



Conclusions & future work

Future work

- We believe that complexity of algorithm is lower than $O(\Delta^2 m)$. Conjecture: $O(\Delta m)$
- Study lower bounds of the problem for distributed scheduler